

On the Origin of Gravitational Wave Sources Observed by LIGO/VIRGO

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GALNUC team members

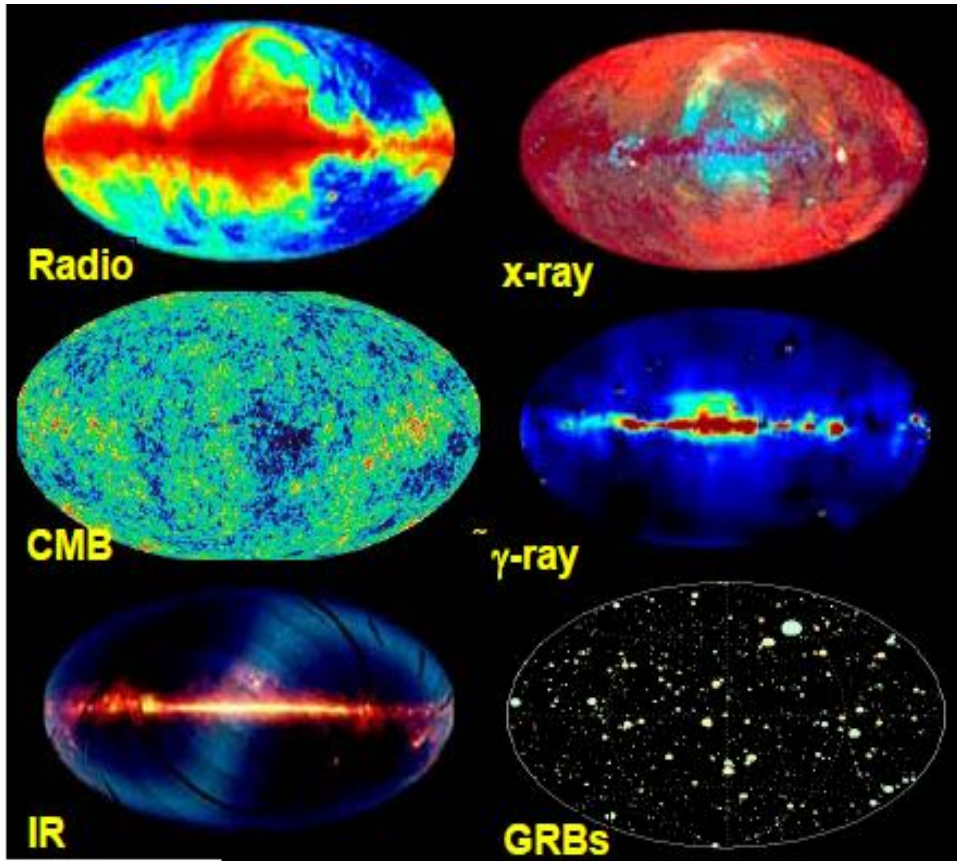
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Scott Tremaine (IAS)



The Dawn of GW astronomy

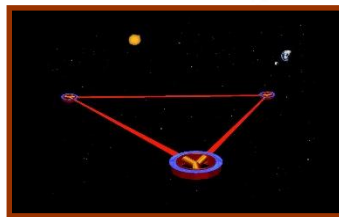
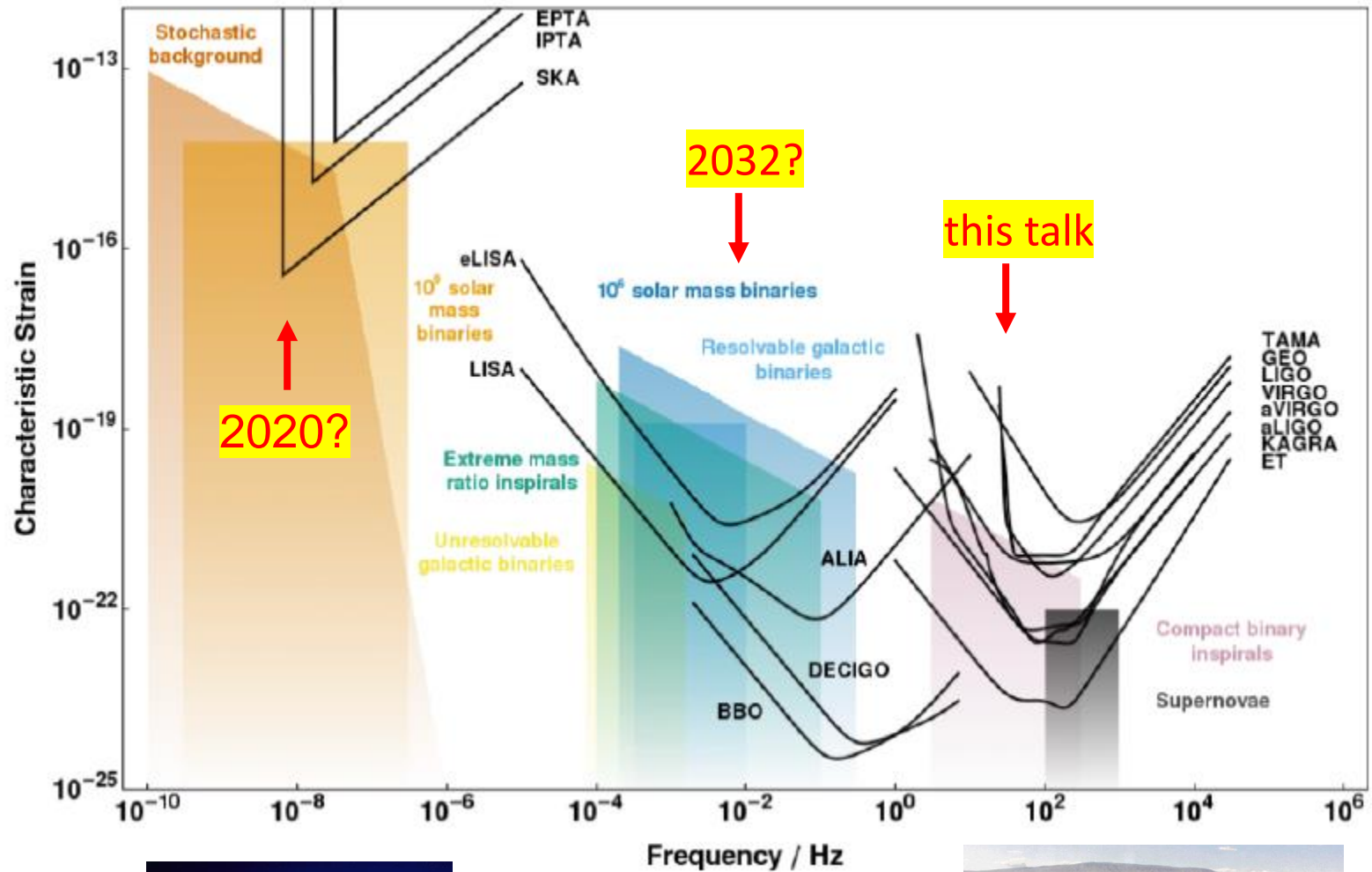


- 1. Status of discoveries
- 2. Does it make sense?
- 3. Astrophysical channels
 - problems with interpretation
- 4. New ideas
- 5. Distinguishing sources

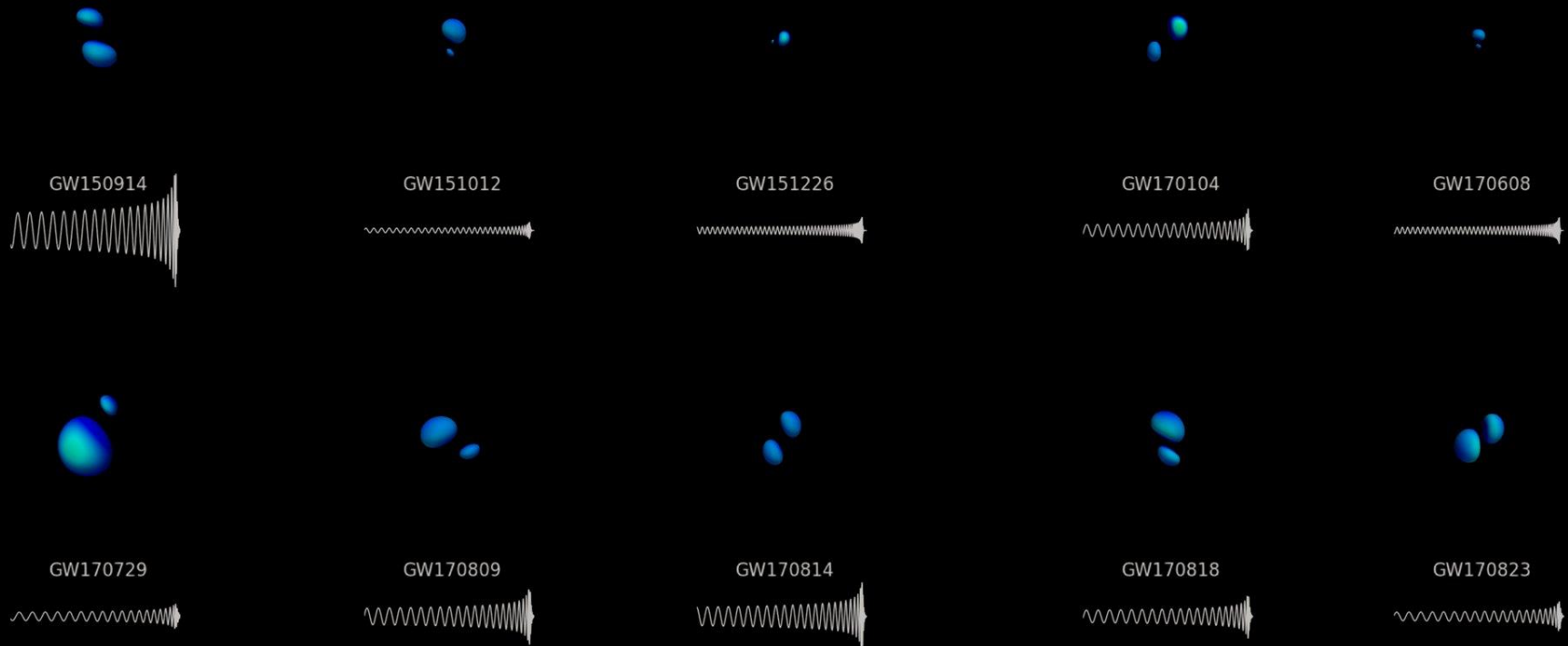
GW sky??

EXPECT THE UNEXPECTED!

Gravitational wave detectors

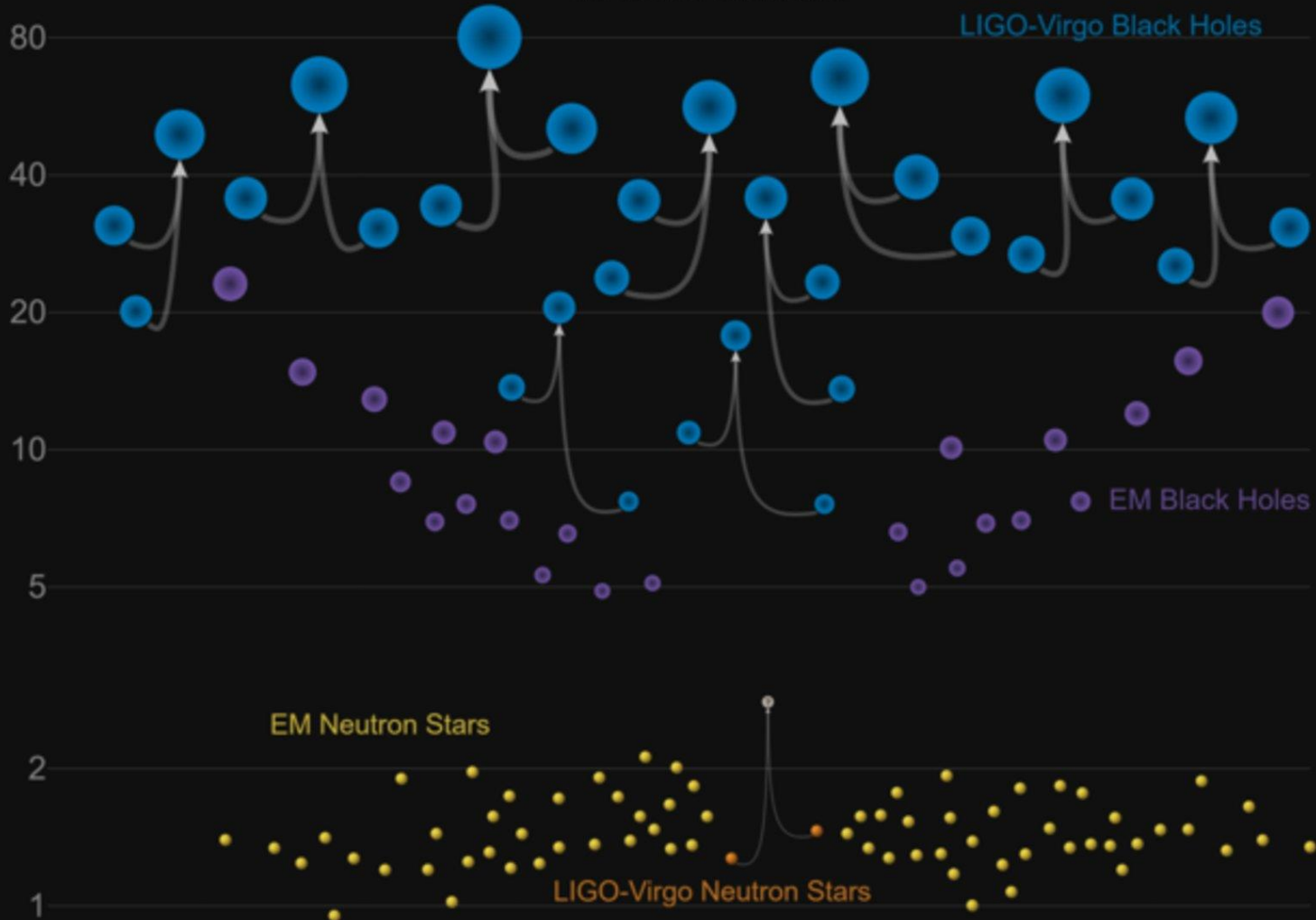


Gravitational wave detections



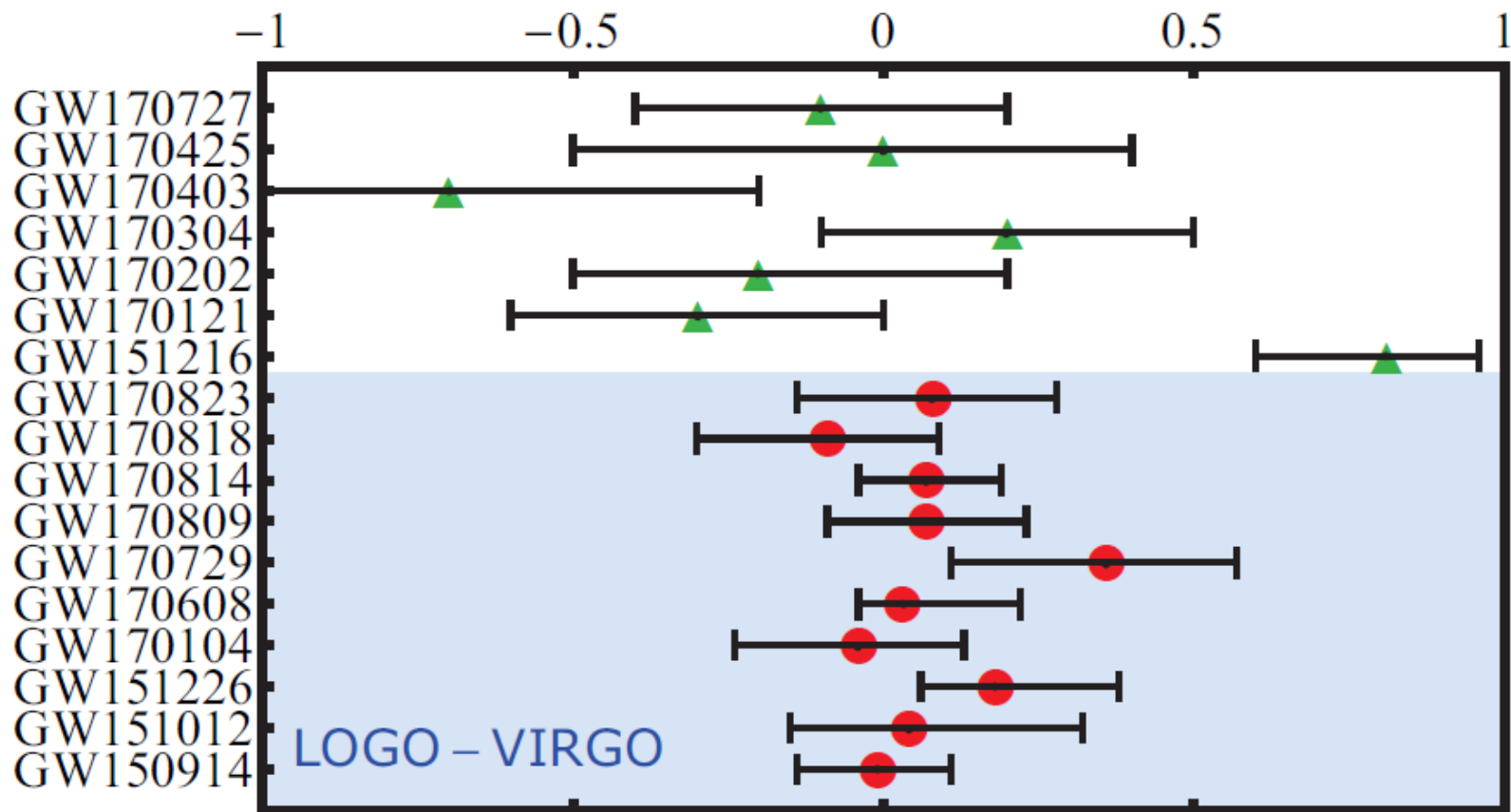
Masses in the Stellar Graveyard

in Solar Masses



Spins

$$\chi_{\text{eff}} = \frac{(m_1 \chi_1 \cos \theta_1 + m_2 \chi_2 \cos \theta_2)}{M}$$



Rate of BBH coalescence

GW150914+LVT151012:

$2 - 600 \text{ Gpc}^{-3} \text{ yr}^{-1}$

+GW151226:

$9 - 240 \text{ Gpc}^{-3} \text{ yr}^{-1}$

+GW170104:

$12 - 213 \text{ Gpc}^{-3} \text{ yr}^{-1}$

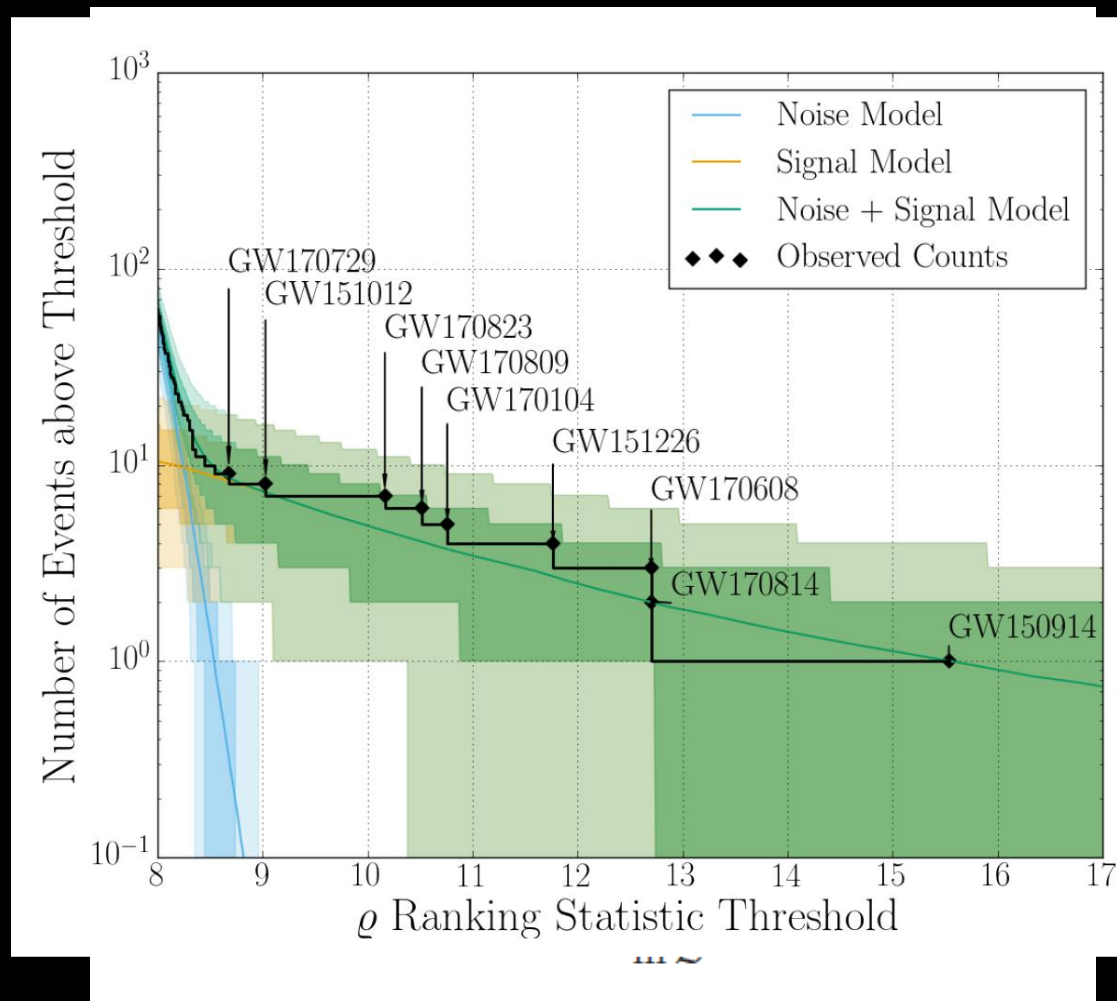
+7 new BH/BH detections:

$29 - 100 \text{ Gpc}^{-3} \text{ yr}^{-1}$

Rate of NS coalescence

GW170608:

$300 - 4700 \text{ Gpc}^{-3} \text{ yr}^{-1}$

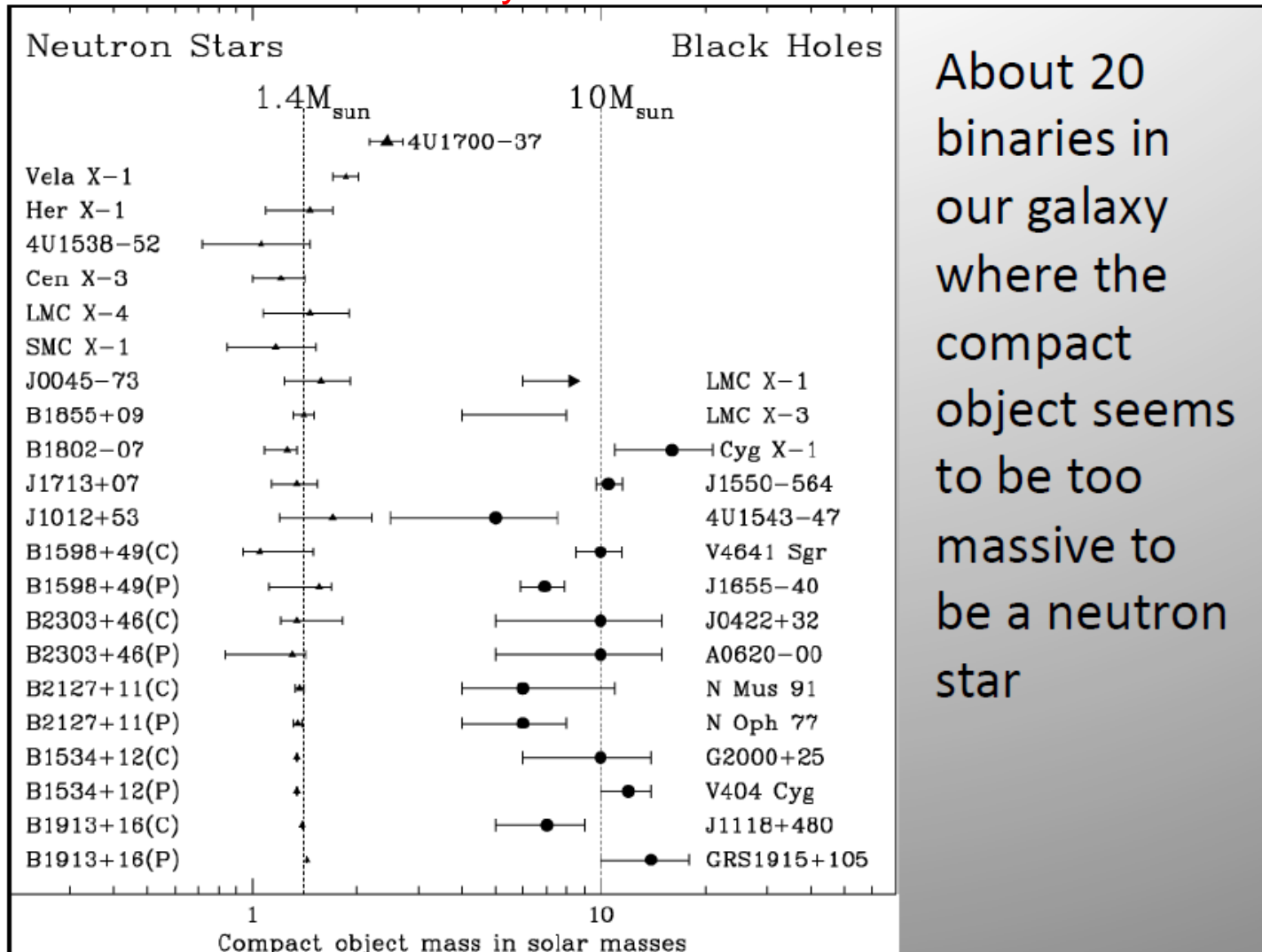


Basic questions

- Does the mass distribution make any sense?
- Does the spin distribution make any sense?
- How did the black holes get so close?
- Do the rates match expectations?

Does the mass distribution make sense?

Observed masses in X-ray binaries

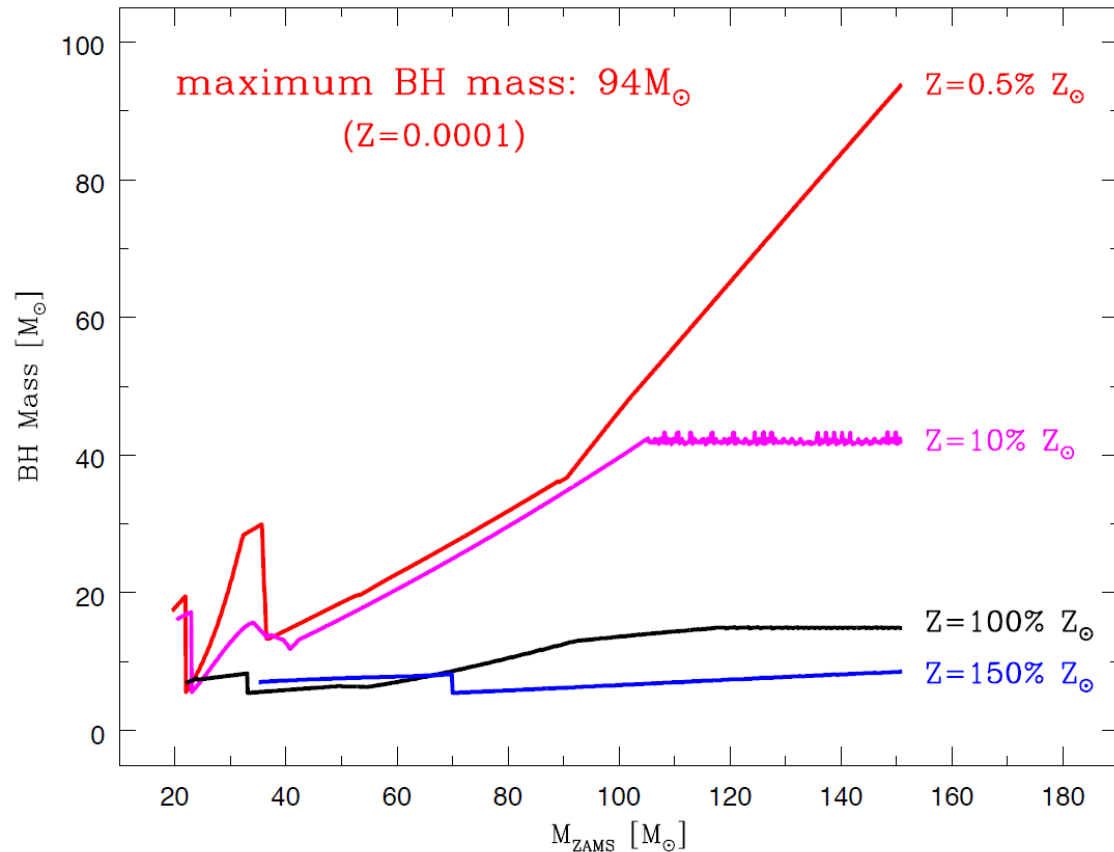


About 20 binaries in our galaxy where the compact object seems to be too massive to be a neutron star

Does the mass distribution make sense?

Theoretical expectations

Belczynski et al. 2010a (ApJ 714, 1217)



– updates:

stellar models: $\sim 130 M_{\odot}$
(Spera et al. 2015)

IMF extension: $\sim 300 M_{\odot}$
(Belczynski et al. 2014)

-(Belczynski et al. 2016):

BH mass down: $\lesssim 50 M_{\odot}$
(pair-instability pulsations)

stellar origin BH can reach: $\sim 100 M_{\odot}$

(Zamperi & Roberts 2009; Mapelli et al. 2009)

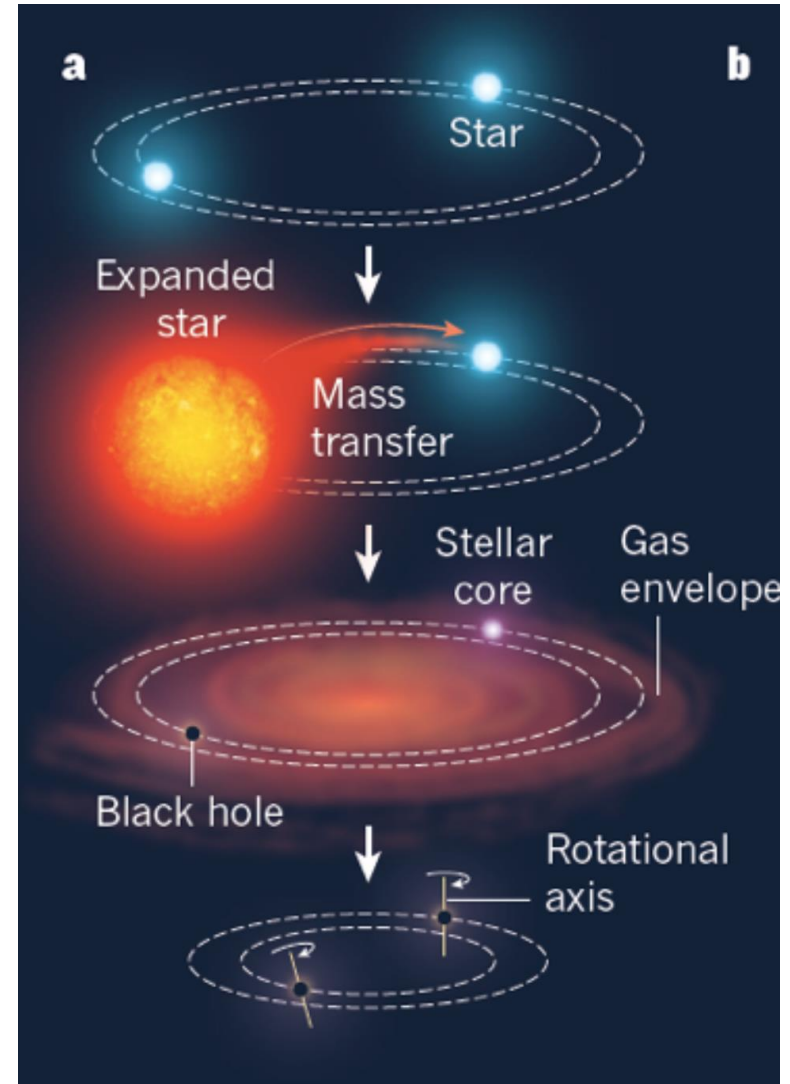


Astrophysical origin of mergers

Option 1: stellar binary evolution

Galactic binaries

- 10^{11} stars in a Milky Way type galaxy
- 10^{7-8} stellar mass black holes
- massive stars in (wide) binaries
 - 25% in triples



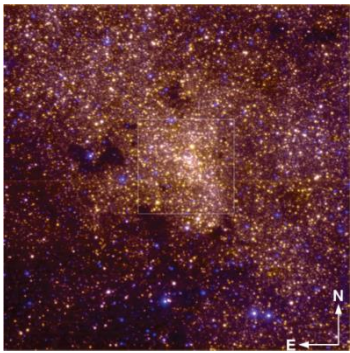
Option 2: Dynamical environments

Globular clusters

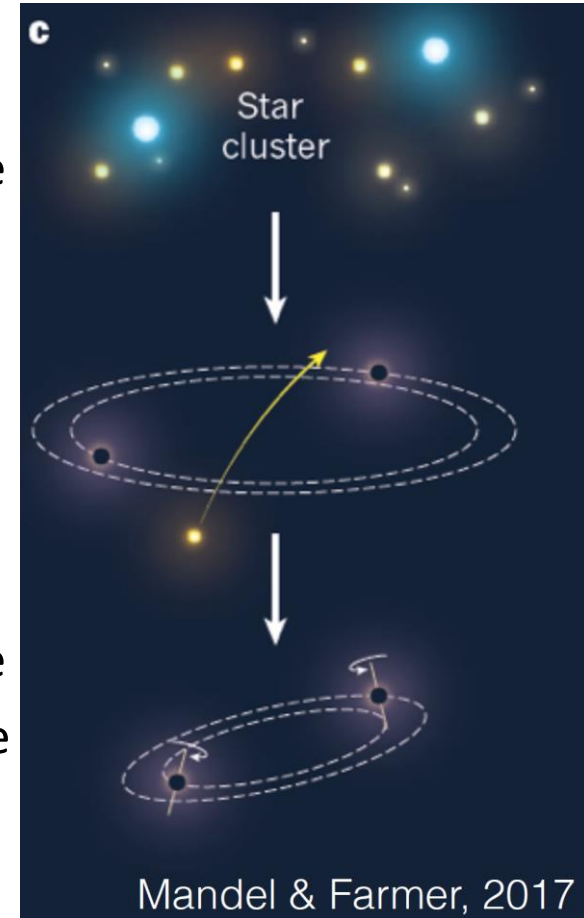


- 0.5% of stellar mass of the Universe
- 100 per galaxy
- Size: 1 pc – 10 pc
- Density 10^3 – 10^5 x higher

Galactic nuclei



- 0.5% of stellar mass of the Universe
- $10^{6-7} M_{\text{sun}}$ **supermassive** black hole
- 10^{4-5} stellar mass black holes
- Size: 1 pc – 10pc
- Density 10^6 – 10^{10} x higher



encounter rate \sim density²

$$\frac{d}{d \ln r} \Gamma = (4\pi r^3) n^2 \sigma_{cs} v$$

Option 3: Dark matter halo

Dark matter halo

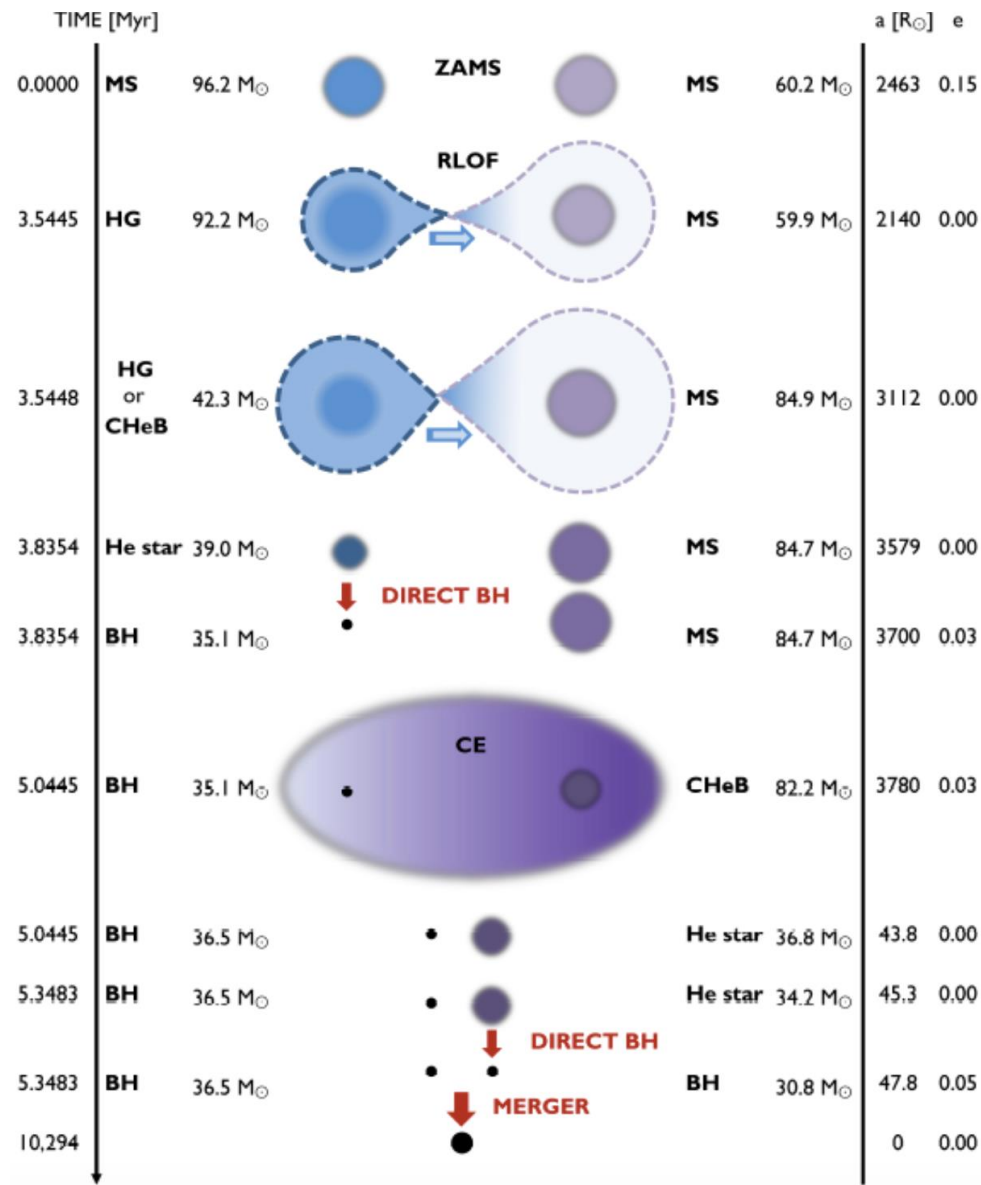
- 10x more mass than in stars
- 10^{10} primordial mass black holes / galaxy?
- Rates match if
 - 100% of dark matter is in 30 Msun **single BHs** (Bird et al 2016)
 - RULED OUT BY OBSERVATION OF a GLOBULAR CLUSTER IN A DWARF GALAXY (Brandt et al. 2017)
 - Newer studies: 1% of dark matter in BHs is sufficient (Ali-Haimud et al 2017)
 - 0.1% of dark matter is in primordial **binary BHs** after inflation (Sasaki et al 2016)
- 30 Msun primordial BHs form when $T \sim 30$ MeV (Carr 1975)
 - standard model does not have any phase transitions at this temperature

Problems

- galactic field binaries: spins, final au problem, common envelope
- galactic field triples: not enough in the right configuration
- globular clusters: not enough black holes
- galactic nuclei: requires multiple mergers/BH, implies spins
- dark matter halos: requires primordial black holes (exotic)

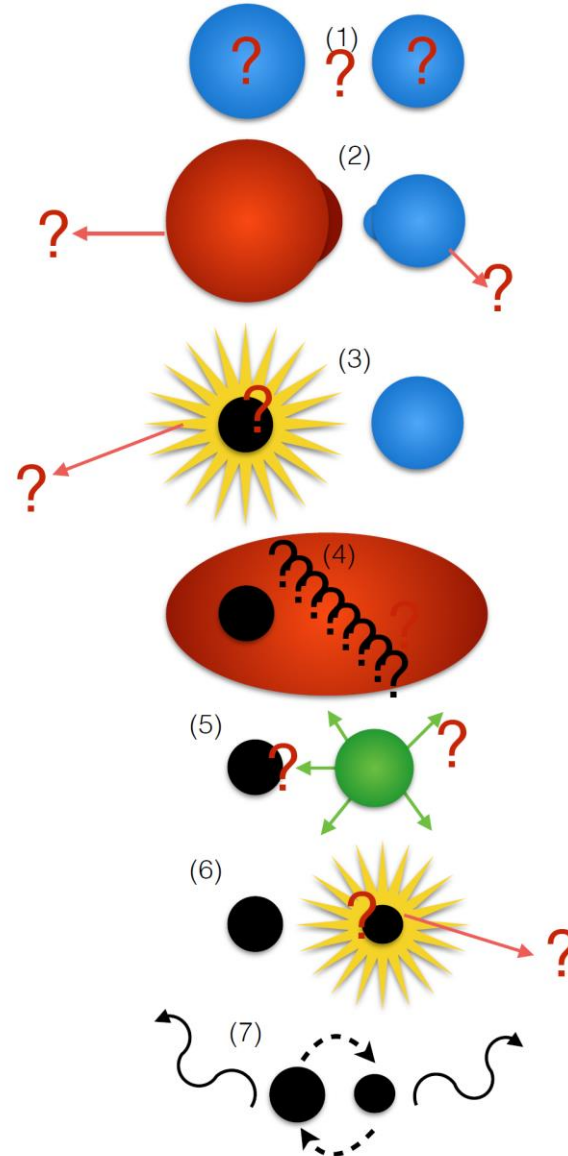
No convincing theory to explain the observed rates!

Option 1: stellar binary evolution



Option 1: stellar binary evolution

Open questions



Option 1: stellar binary evolution

What about spins?

- Black hole X-ray binaries show **evidence of high spins**

Table 1 The masses and spins, measured via continuum-fitting, of ten stellar black holes^a

System	a_*	M/M_\odot	References
Persistent			
Cyg X-1	>0.95	14.8 ± 1.0	Gou et al. 2011; Orosz et al. 2011a
LMC X-1	$0.92^{+0.05}_{-0.07}$	10.9 ± 1.4	Gou et al. 2009; Orosz et al. 2009
M33 X-7	0.84 ± 0.05	15.65 ± 1.45	Liu et al. 2008; Orosz et al. 2007
Transient			
GRS 1915+105	$>0.95^b$	10.1 ± 0.6	McClintock et al. 2006; Steeghs et al. 2013
4U 1543-47	0.80 ± 0.10^b	9.4 ± 1.0	Shafee et al. 2006; Orosz 2003
GRO J1655-40	0.70 ± 0.10^b	6.3 ± 0.5	Shafee et al. 2006; Greene et al. 2001
XTE J1550-564	$0.34^{+0.20}_{-0.28}$	9.1 ± 0.6	Steiner et al. 2011; Orosz et al. 2011b
H1743-322	0.2 ± 0.3	$\sim 8^c$	Steiner et al. 2012a
LMC X-3	$<0.3^d$	7.6 ± 1.6	Davis et al. 2006; Orosz 2003
A0620-00	0.12 ± 0.19	6.6 ± 0.25	Gou et al. 2010; Cantrell et al. 2010

^aErrors are quoted at the 68 % level of confidence, except for the three spin limits, which are estimated to be at the 99.7 % level of confidence.

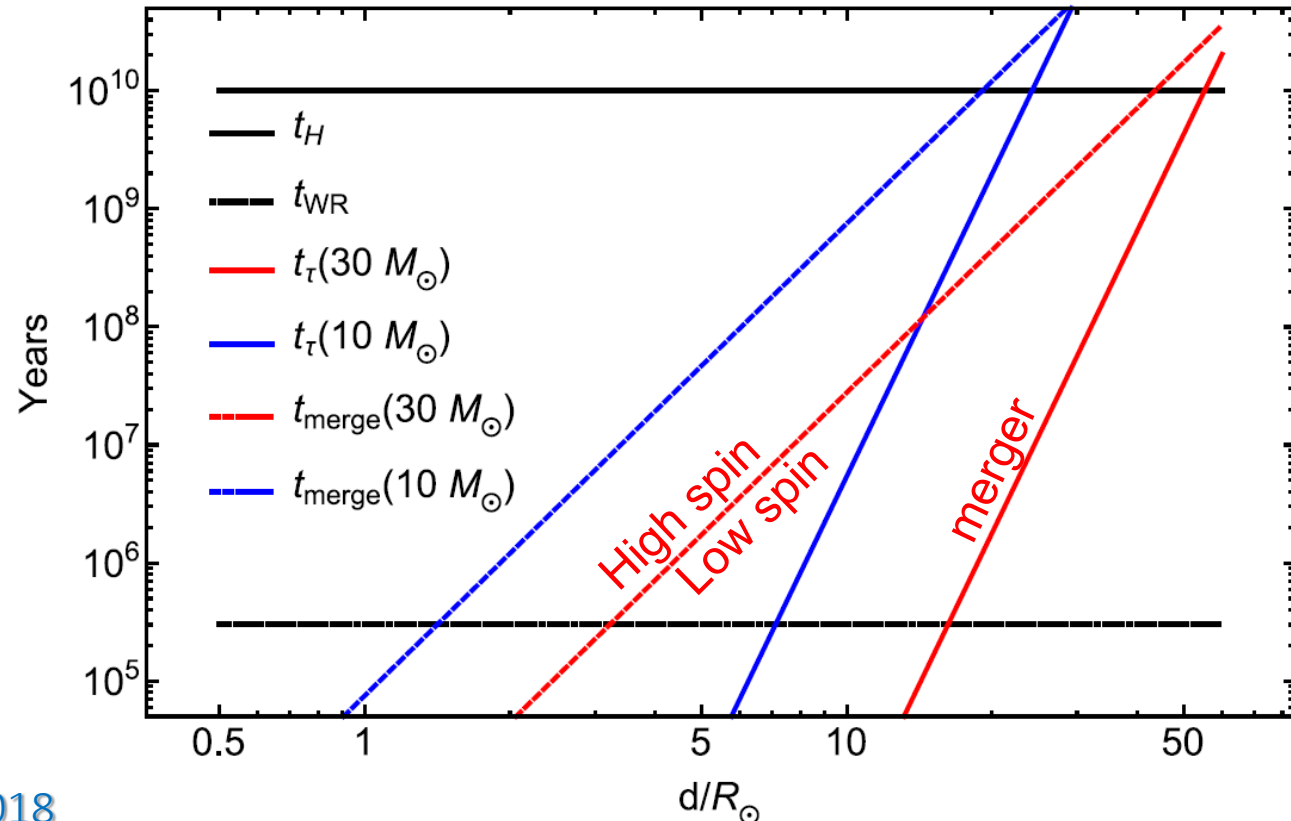
^bUncertainties greater than those in papers cited because early error estimates were crude.

^cMass estimated using an empirical mass distribution (Özel et al. 2010).

^dPreliminary result pending improved measurements of M and i .

Option 1: stellar binary evolution

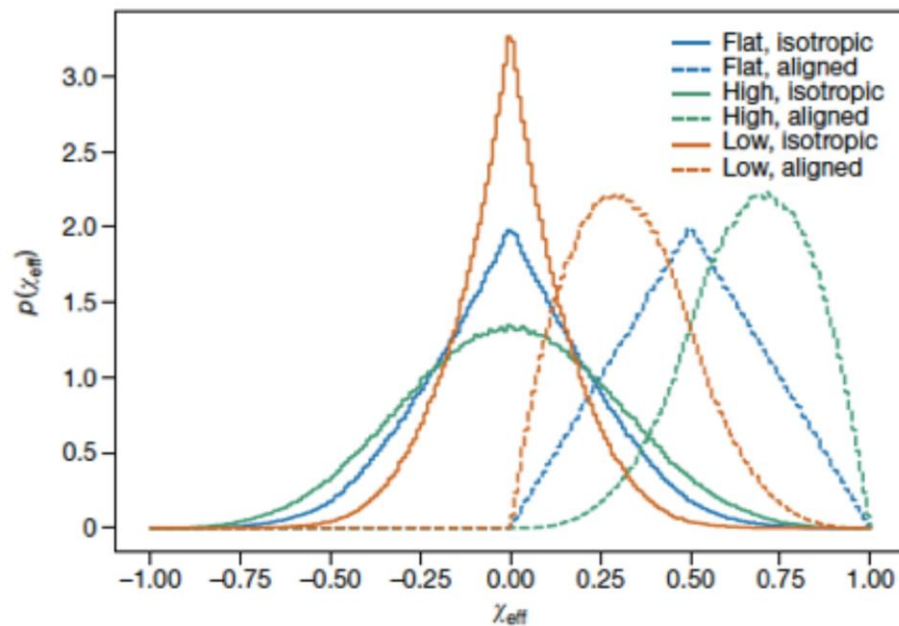
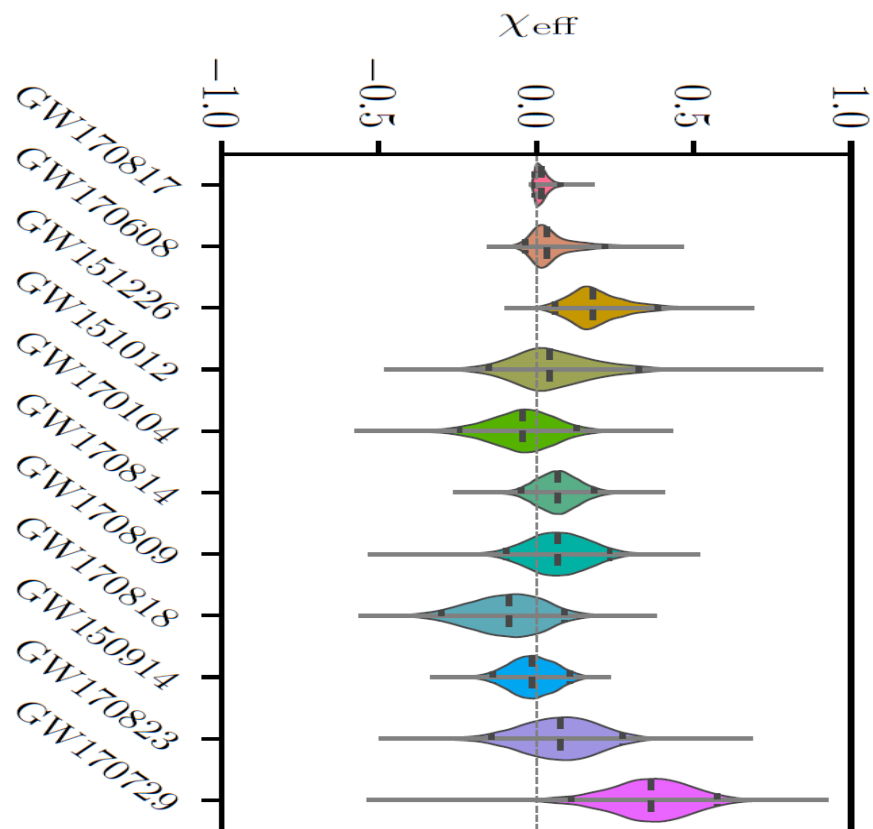
- Progenitor WR star is spun up to high spins?
- What is black hole spin after formation?
- Spin up from accretion?



Option 1: stellar binary evolution

What about spins?

- LIGO distribution **inconsistent** with aligned **high spins**



$$\chi_{\text{eff}} = \frac{(m_1 \chi_1 \cos \theta_1 + m_2 \chi_2 \cos \theta_2)}{M}$$

Option 1: stellar binary evolution

What about the rates?

- Theory very uncertain – consistent with observations
- Relative rate of NS/NS mergers vs. BH/BH mergers may be a problem

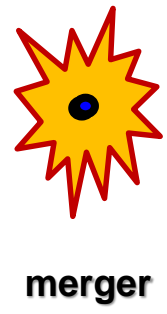
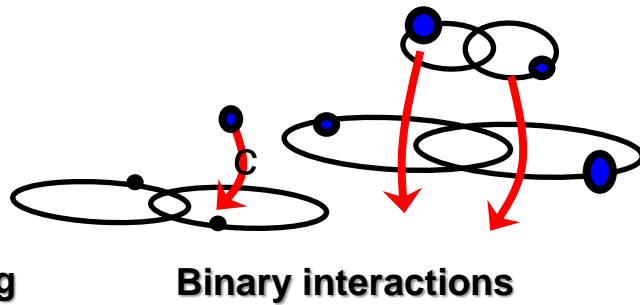
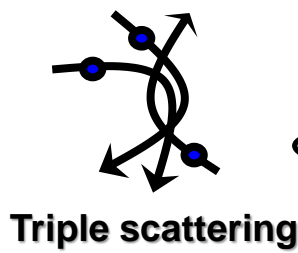
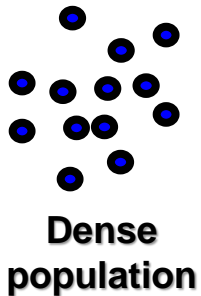
Option 2: dynamical environments

- A theoretically clean problem: N-body



Option 2: dynamical environments

- A theoretically clean problem: N-body



- binary formation from singles
- exchange interactions
- mass segregation

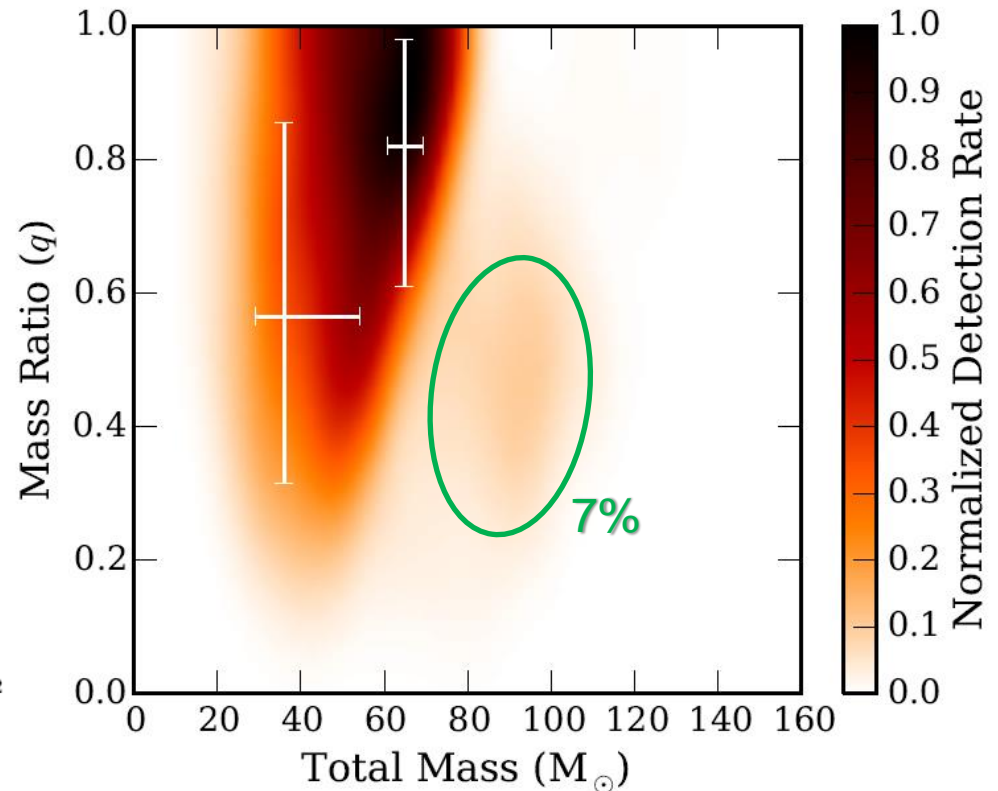
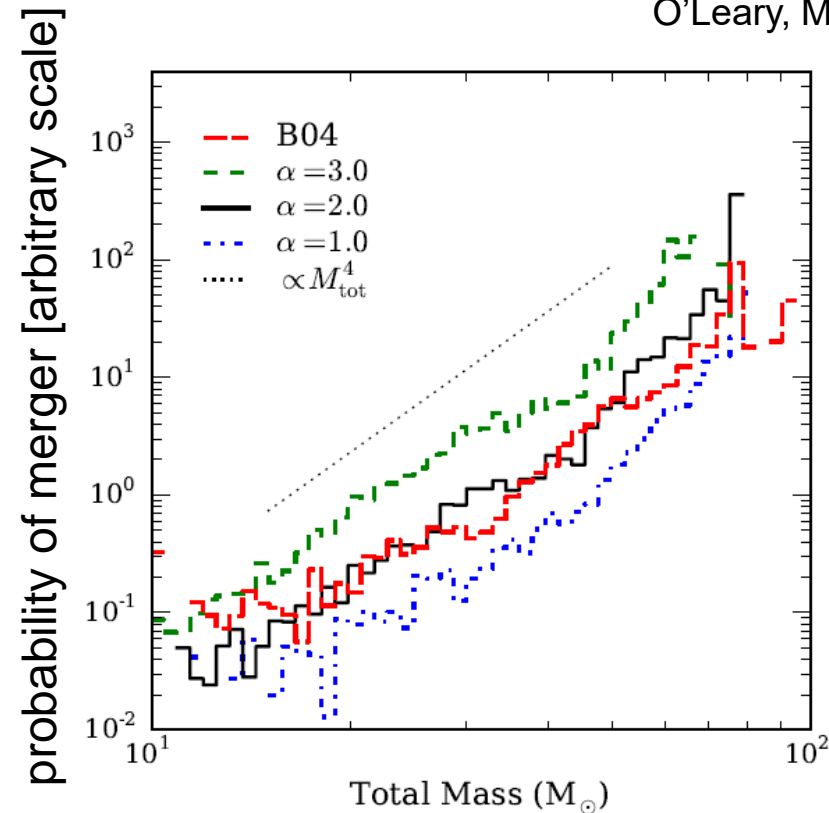
Expectation:

Merger probability larger for heavier objects

Mass distribution for globular clusters

Monte Carlo and Nbody simulations

O'Leary, Meiron, Kocsis (2016) (see also Rodriguez+ '18, Askar+ '18)

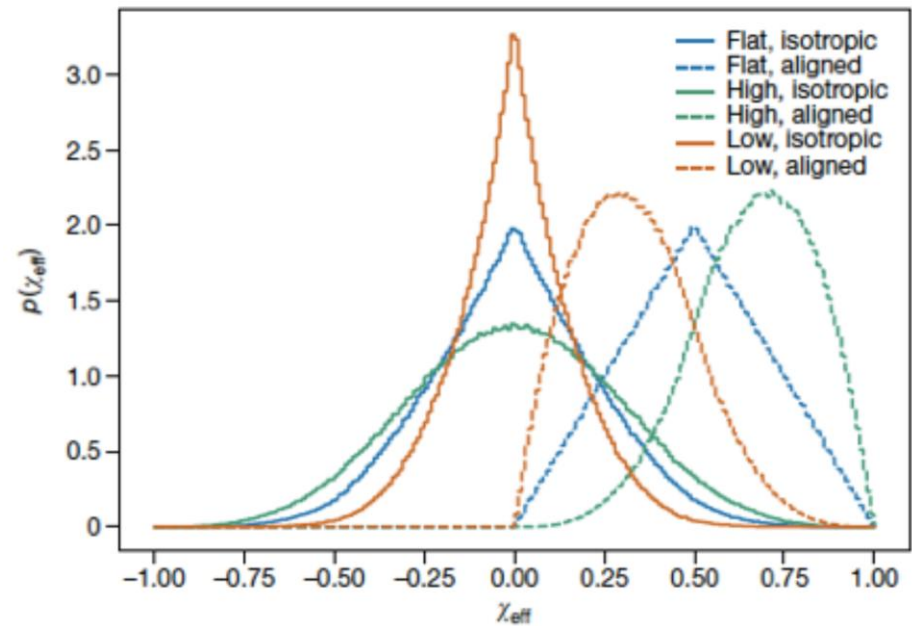
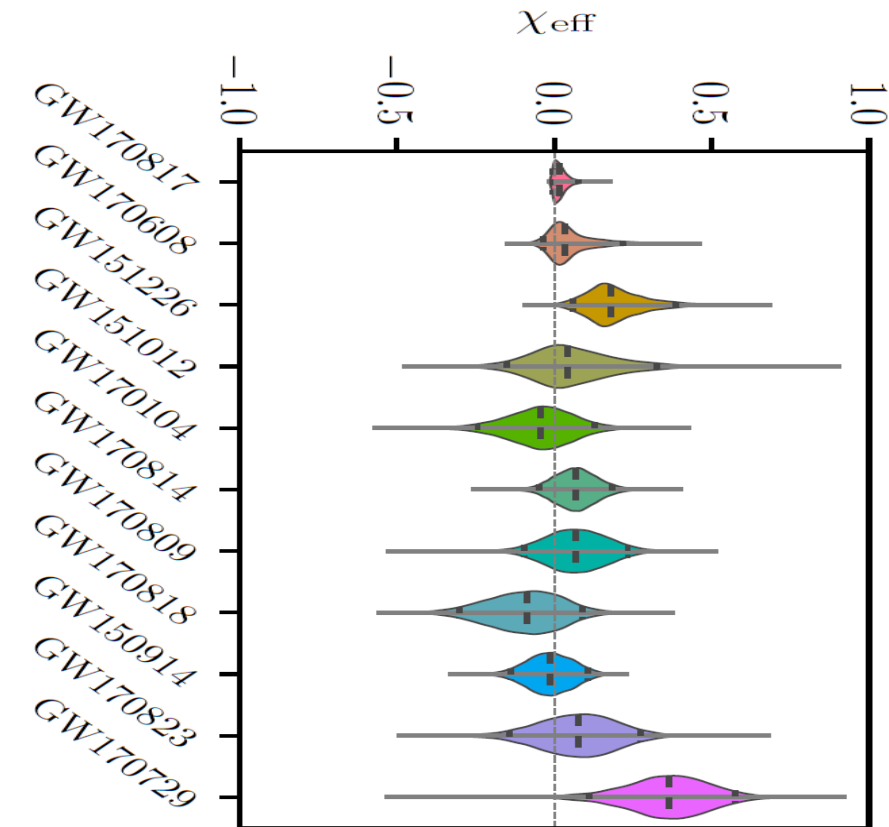


Robust statement (independent of IMF): heavy objects **merge more often M^4**

Option 2: dynamical environments

What about spins?

- LIGO distribution **consistent** with isotropically distributed **spins**



$$\chi_{\text{eff}} = \frac{(m_1 \chi_1 \cos \theta_1 + m_2 \chi_2 \cos \theta_2)}{M}$$

Option 2: dynamical environments

What about the rates?

Expected rates (MCMC and Nbody simulations): $\sim 6 \text{ Gpc}^{-3} \text{ yr}^{-1}$

Simple upper limit:

- assume **each** BH merges **at most once*** in a Hubble time
- BHs form from stars with $m > 20 M_{\text{Sun}}$, $dN/dm \sim m^{-2.35}$
→ 0.3% of stars turns into BHs

– **globular clusters: $R < 40 \text{ Gpc}^{-3} \text{ yr}^{-1}$**

- 0.5% of stellar mass, $10^{5.5}$ stars with $n \sim 0.8 \text{ Mpc}^{-3}$

– **galactic nuclei: $R < 35 \text{ Gpc}^{-3} \text{ yr}^{-1}$**

- 0.5% of stellar mass, 10^7 stars with $n \sim 0.02 \text{ Mpc}^{-3}$

* note: in simulations **20%** of BHs **form binaries** and only **50%** of binaries merge

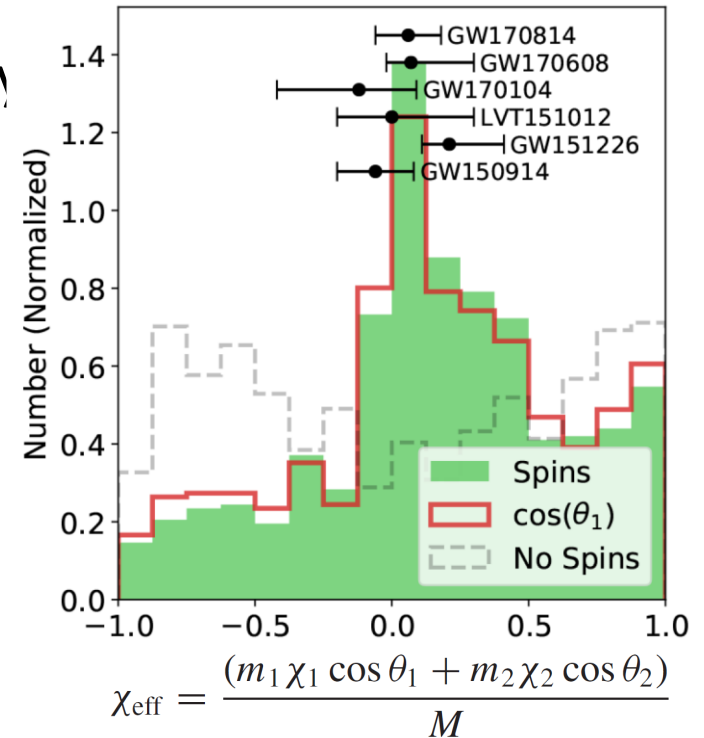
Observed rate: $29 - 100 \text{ Gpc}^{-3} \text{ yr}^{-1}$

(powerlaw mass distribution prior, Abbott+ 2018 arxiv:1811.12907)

Option 3: triples

Tertiary perturber:

- Kozai-Lidov effect increases eccentricity
→ merger
- Spins **align in the perpendicular** direction
- expected **rates are**
 $2 - 25 \text{ Gpc}^{-3} \text{ yr}^{-1}$



Summary of channels and rates

- galactic field binaries: spins, final au problem, common envelope
- galactic field triples: not enough in the right configuration
- globular clusters: not enough black holes
- galactic nuclei: requires multiple mergers/BH, implies spins
- dark matter halos: requires primordial black holes (exotic)

No convincing theory to explain the observed rates!

Problems

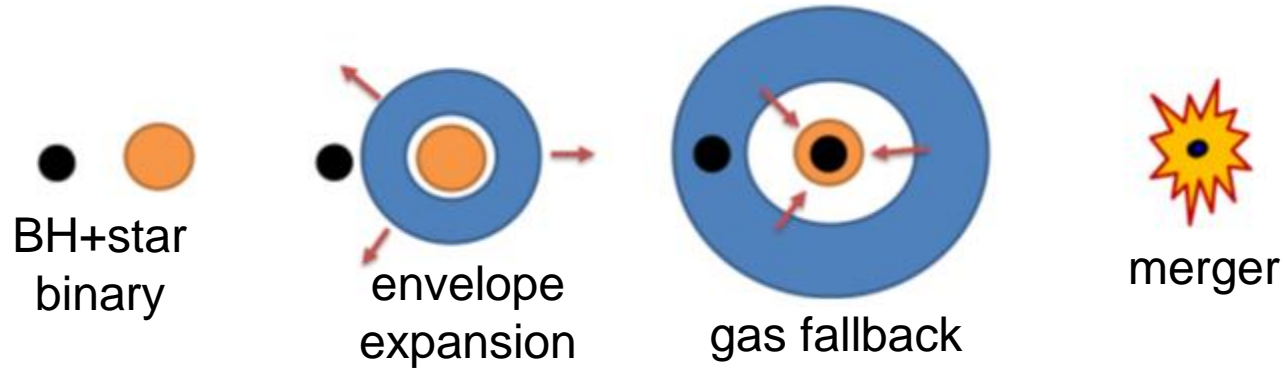
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possible ways forward
I.

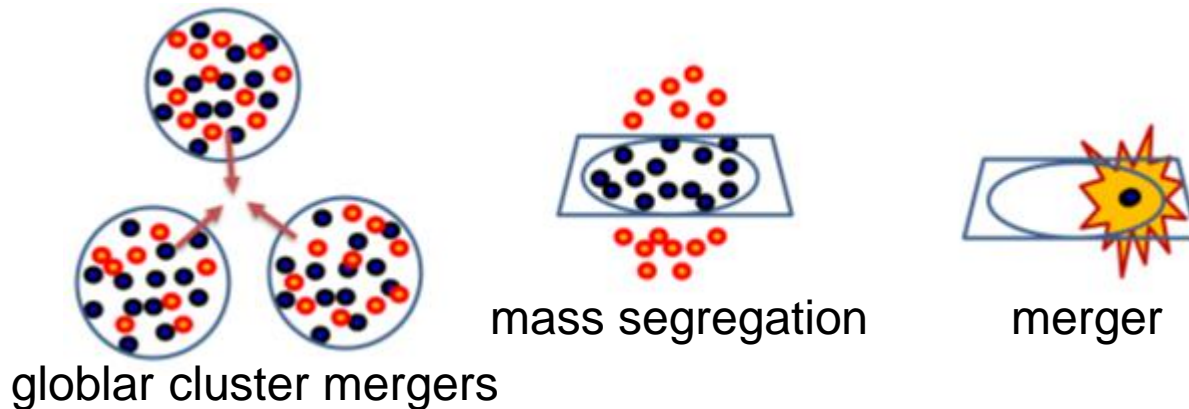
New ideas

1. Gas fallback mergers (Tagawa, Saitoh, & Kocsis, PRL 2018)

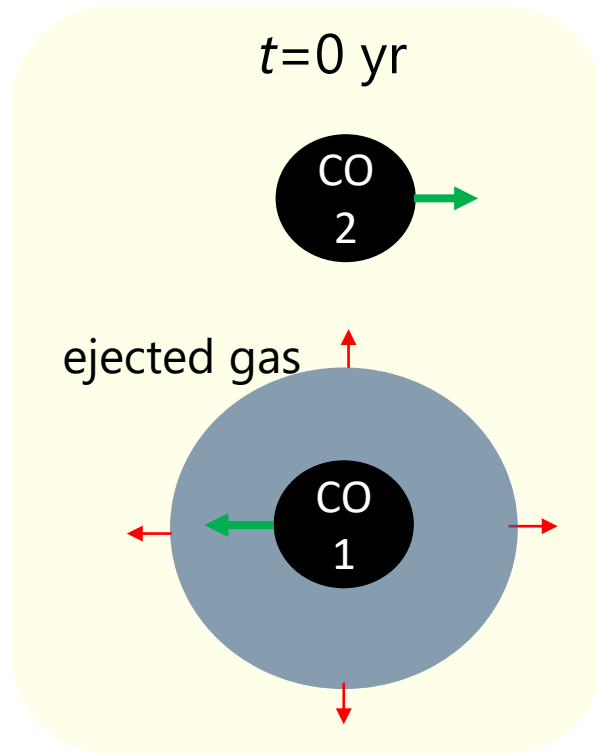


2. Disrupted globular clusters (Fragione & Kocsis, PRL 2018)

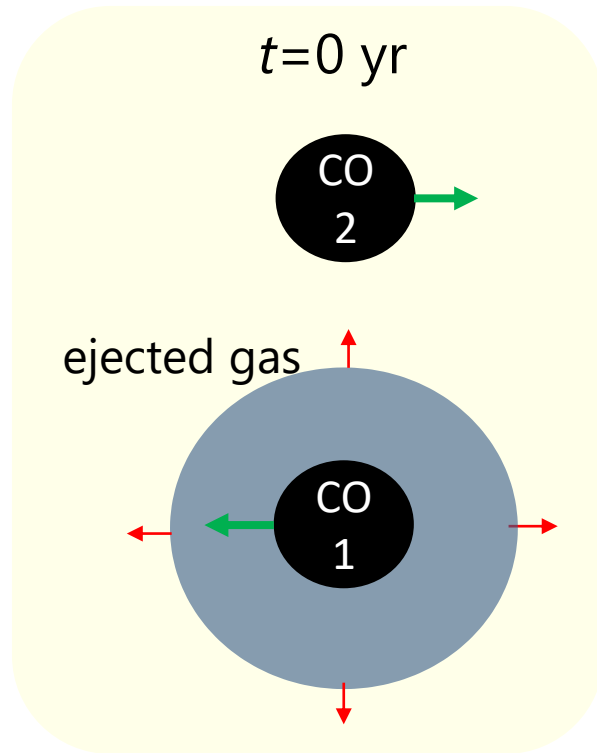
3. Black hole disks (Szolgyen & Kocsis PRL 2018)



Fallback driven merger



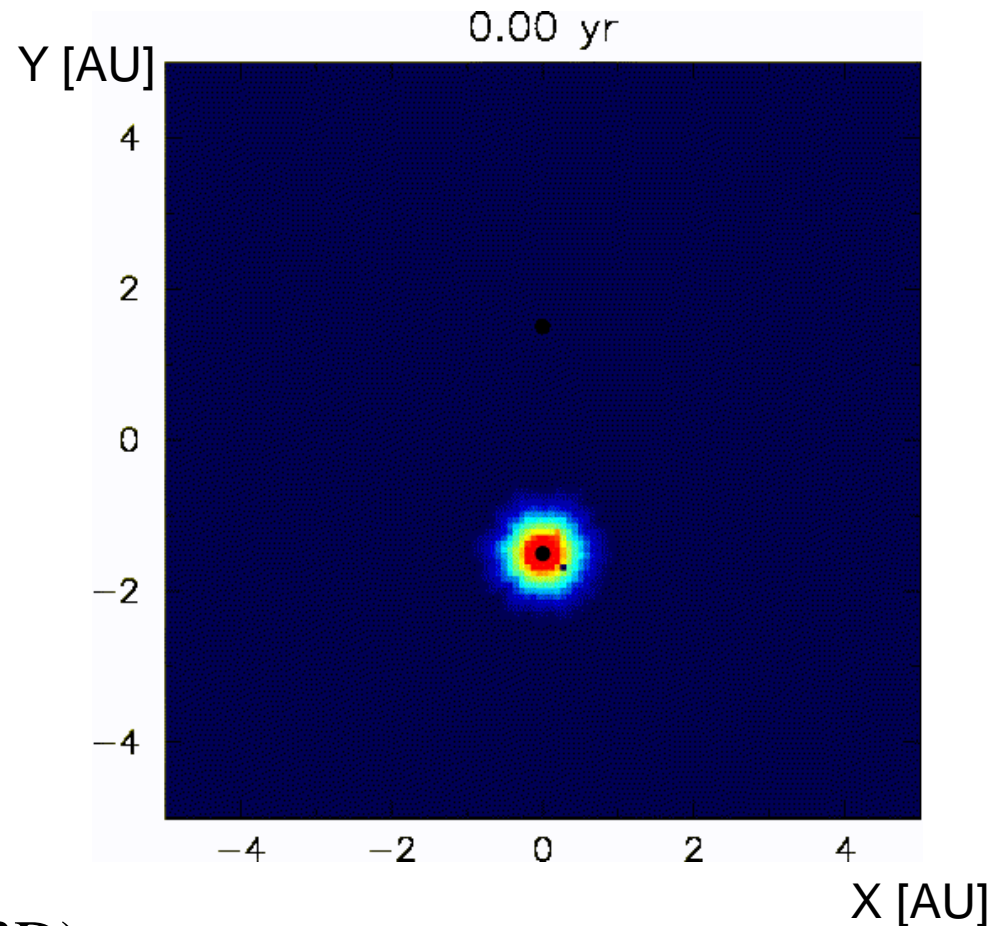
Fallback driven merger



N-body/SPH simulation (3D)

Ideal gas EOS

$$v(r) = v_{\max} r/r_{\max}$$



Initial condition:

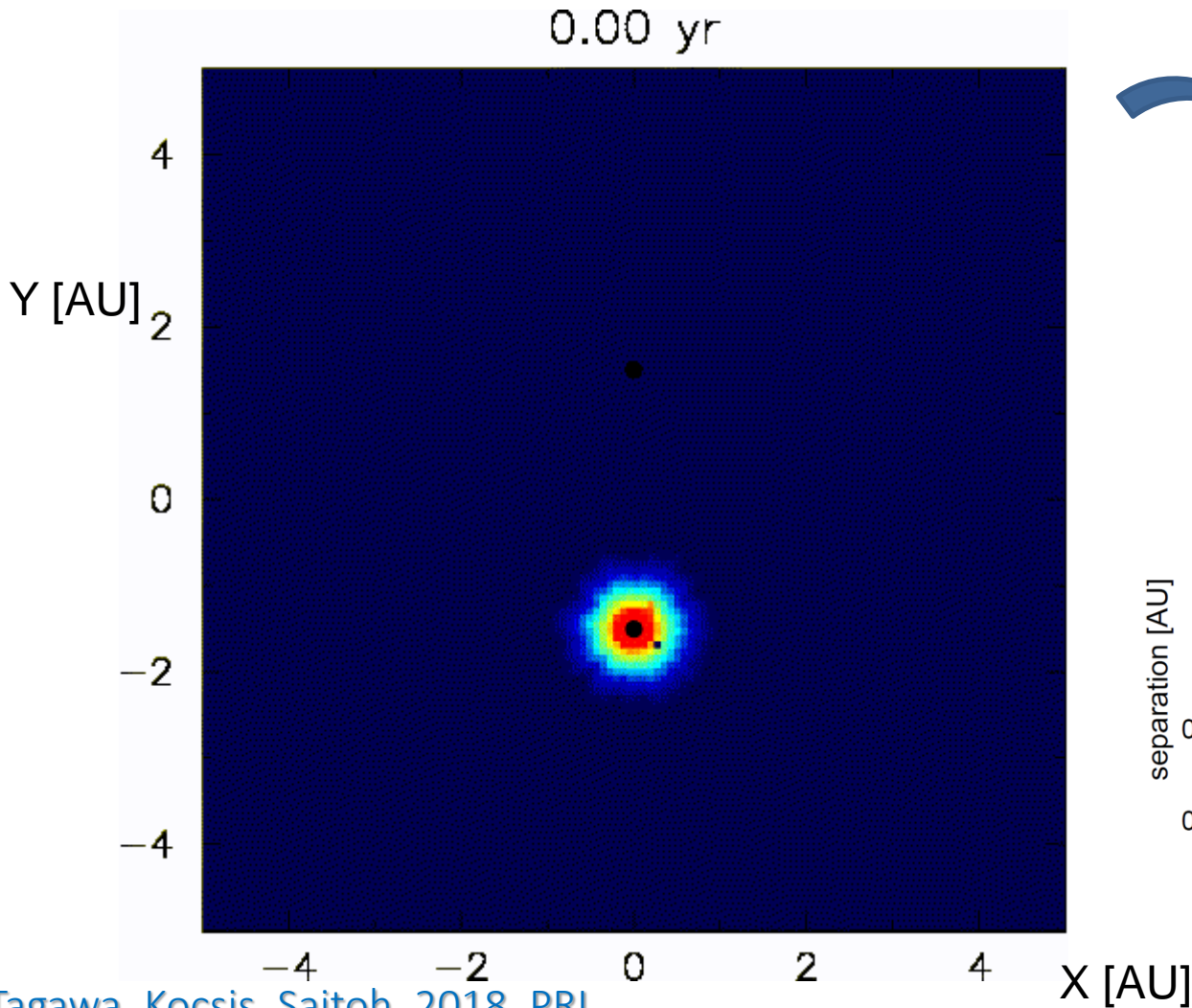
studies of fallback accretion

e.g. Zampieri et al. 1998, Batta et al. 2017

Fallback driven merger

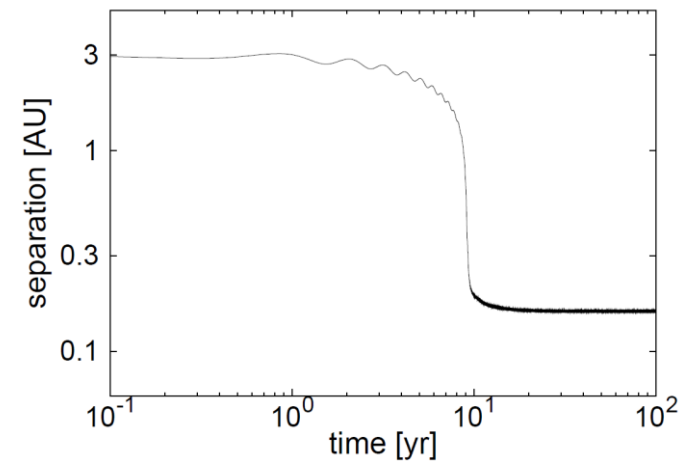


$$M_{CO1} = M_{CO2} = 5M_{\odot}$$
$$M_{gas,ini} = 5.4M_{\odot}$$



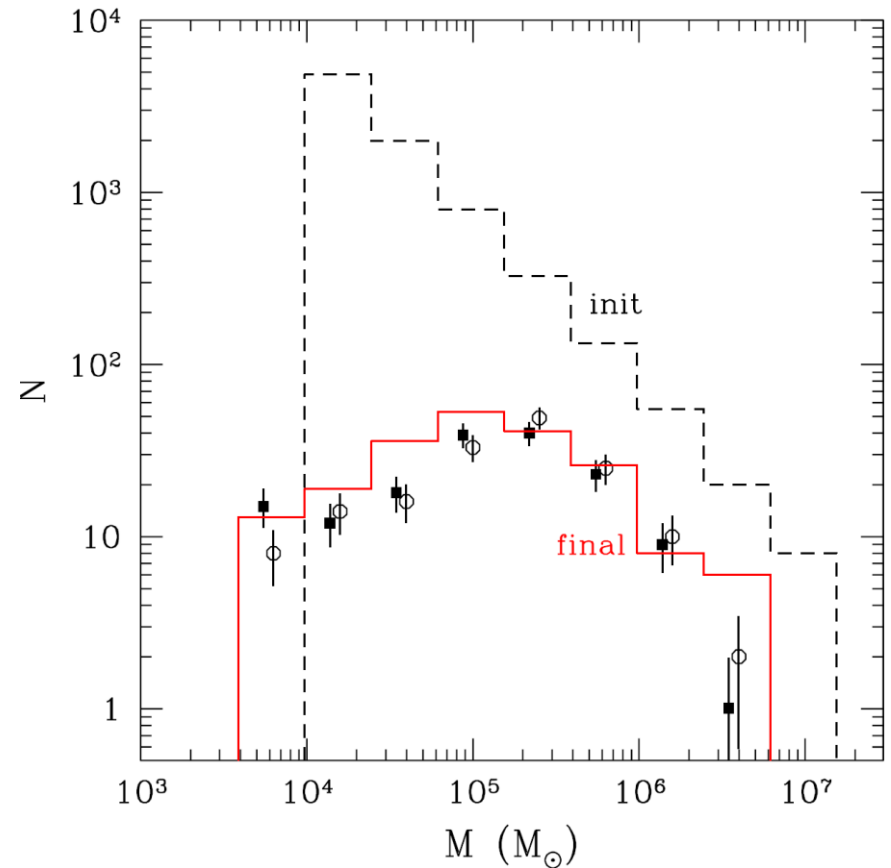
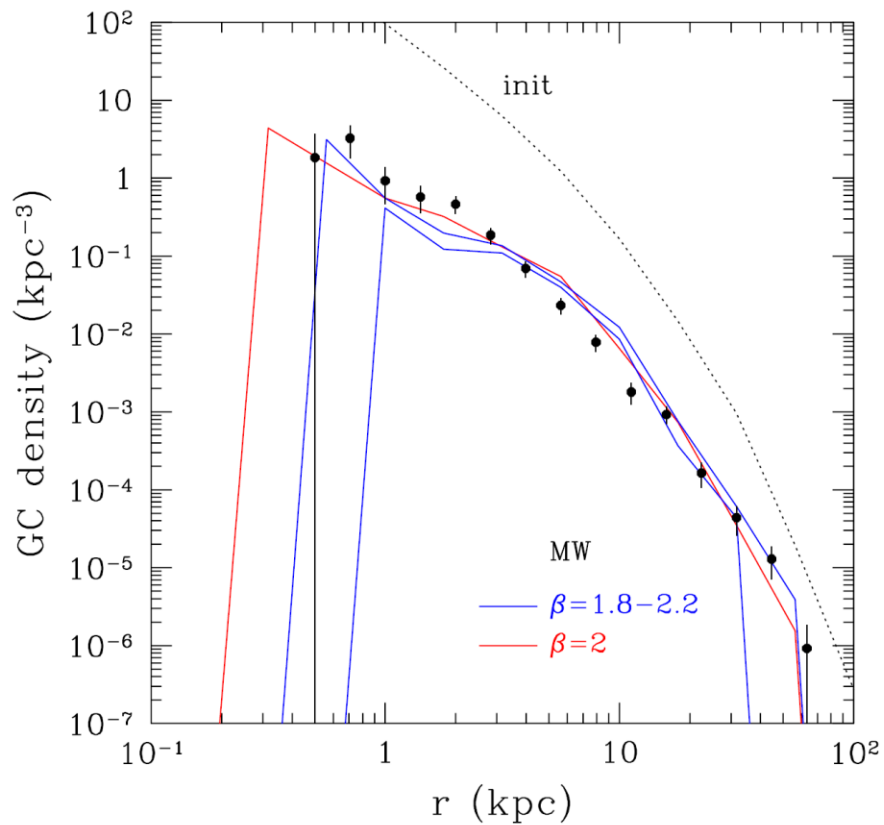
rotating clockwise

A blue curved arrow pointing downwards and to the right, indicating clockwise rotation.



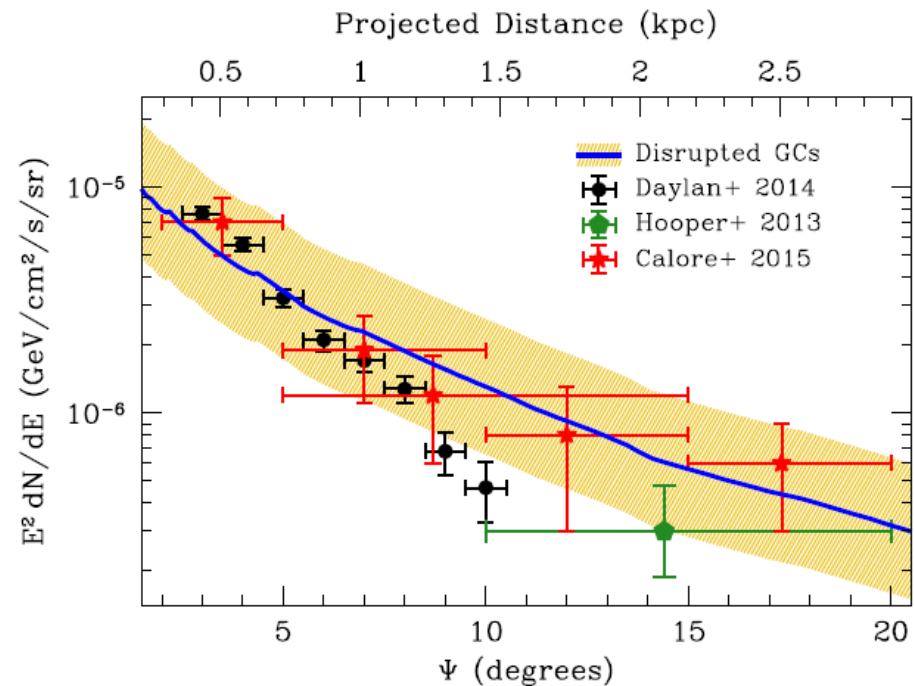
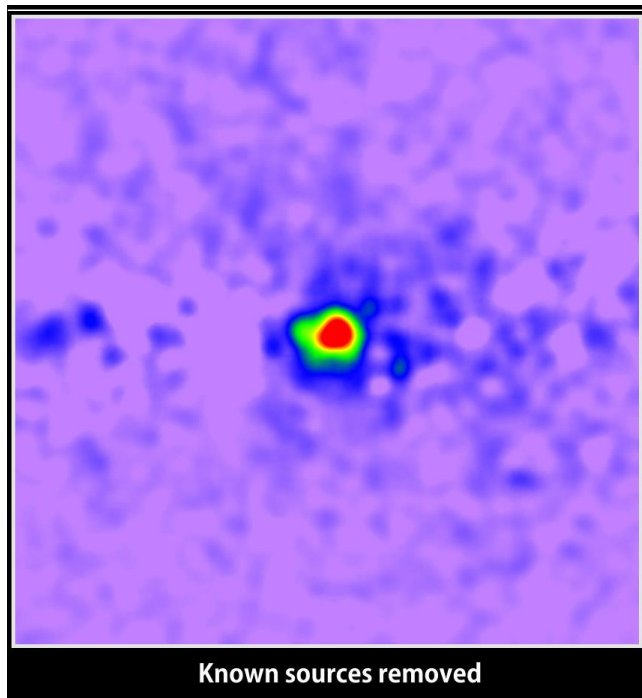
Disrupted globular clusters

- Globular clusters were much more numerous in the past



Disrupted globular clusters

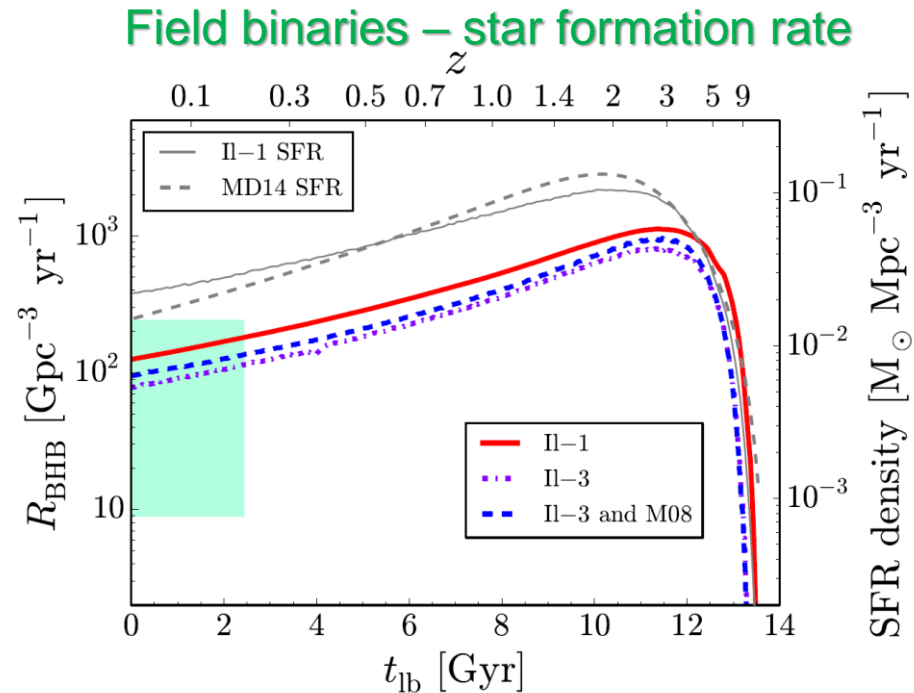
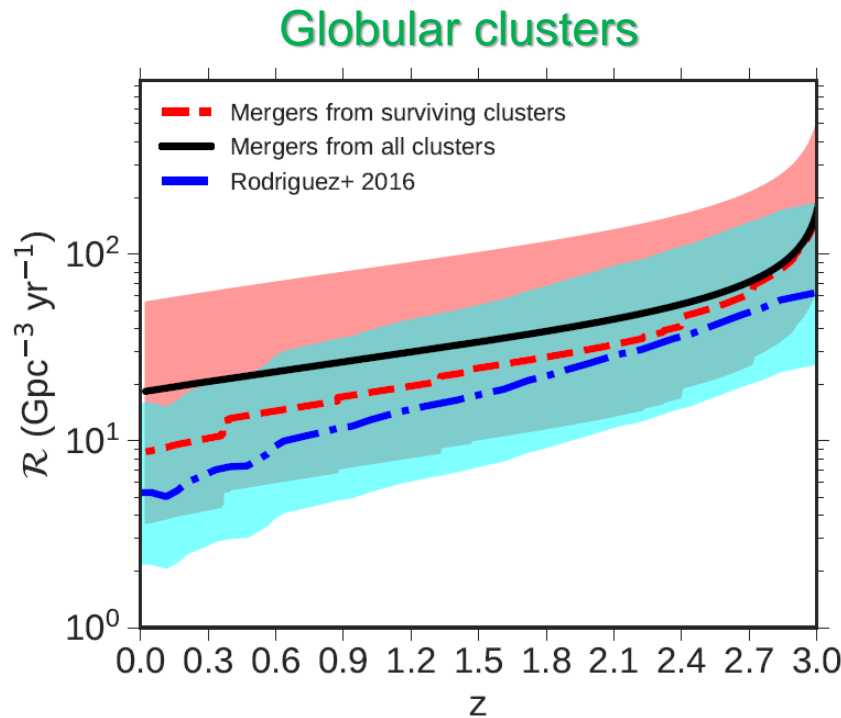
- Gamma rays from disrupted globular clusters explains “Fermi excess”



Brandt, Kocsis (2015)

Disrupted globular clusters

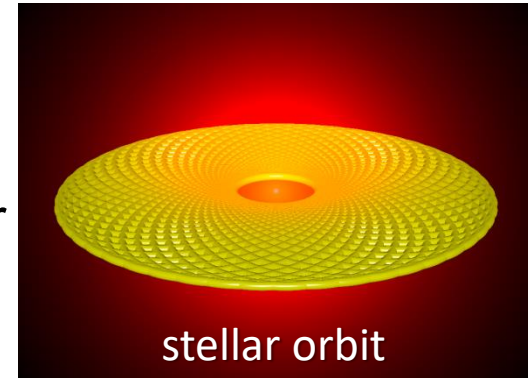
- Implications for LIGO
 - High rates from disrupted globular clusters



Black hole disks

Motion of stars in the galactic disk:

- Elliptic orbit around supermassive black hole
- Precession due to spherical component of star cluster



Orbital planes reorient and relax very quickly

Long term gravitational interaction
of stellar orbits

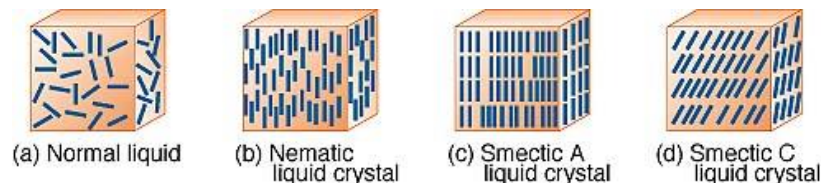
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Interaction among liquid crystal
molecules

(Kocsis+Tremaine 2015, Kocsis+Tremaine in prep., Roupas+Kocsis+Tremaine in prep)

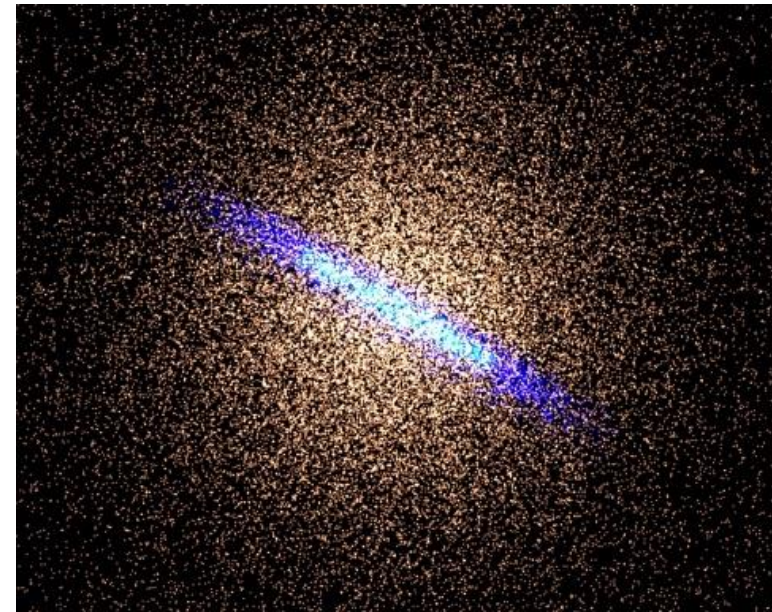
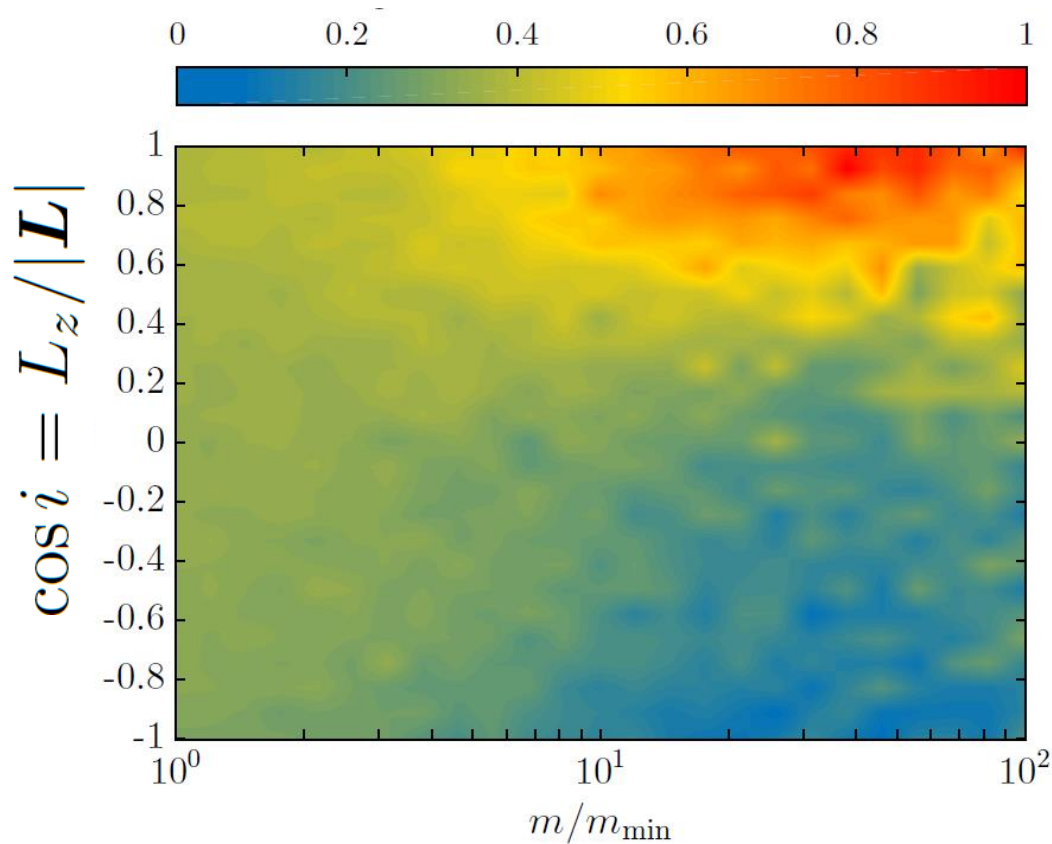
Maximum entropy:

- massive objects: ordered phase
- light objects: spherical phase
- Implication: Black hole disks !



Black hole disks in galactic nuclei

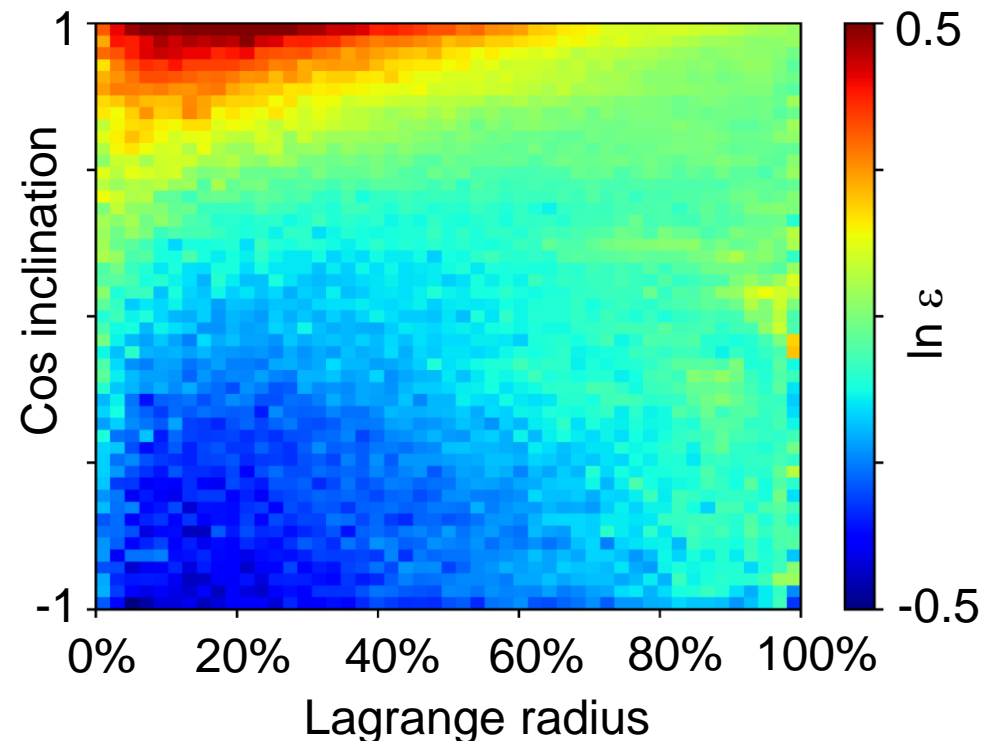
- Massive objects like black holes sink to form a disk
 - mergers more likely



Szolgyen, Kocsis PRL 2018

Black hole disks in globular clusters

- Does this happen in globular clusters? – yes!
- Average mass at a given inclination and radius relative to average mass at a given radius



Average mass at a given inclination and radius relative to average mass at given radius

$$\varepsilon(r, \cos i) \equiv \frac{\bar{m}(r, \cos i)}{\bar{m}(r)}$$

**possible ways forward
II.**

Distinguishing sources

from different channels

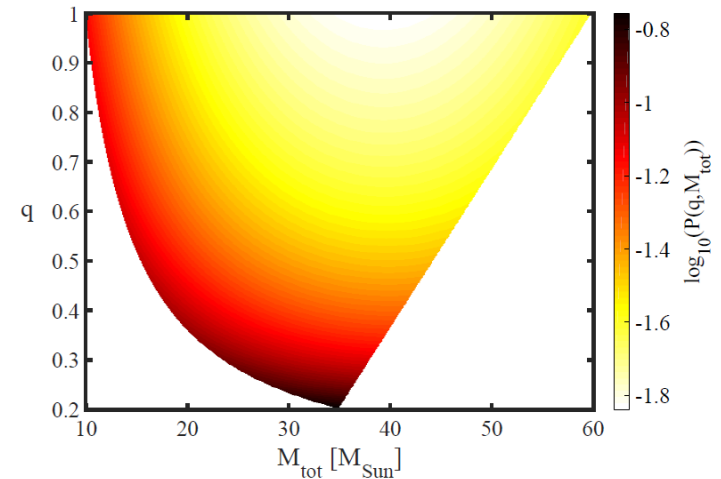
- eccentricity, mass, spin distribution
- electromagnetic counterparts
- intermediate mass black holes

Mass distribution for different processes

universal diagnostic: independent of the mass function

Given: $\mathcal{R}(m_1, m_2) \propto \mathcal{L}(m_1, m_2) f(m_1) f(m_2)$

How can we eliminate the unknown $f(m)$?



Mass distribution for different processes

universal diagnostic: independent of the mass function

Given: $\mathcal{R}(m_1, m_2) \propto \mathcal{L}(m_1, m_2) f(m_1) f(m_2)$

How can we eliminate the unknown $f(m)$?

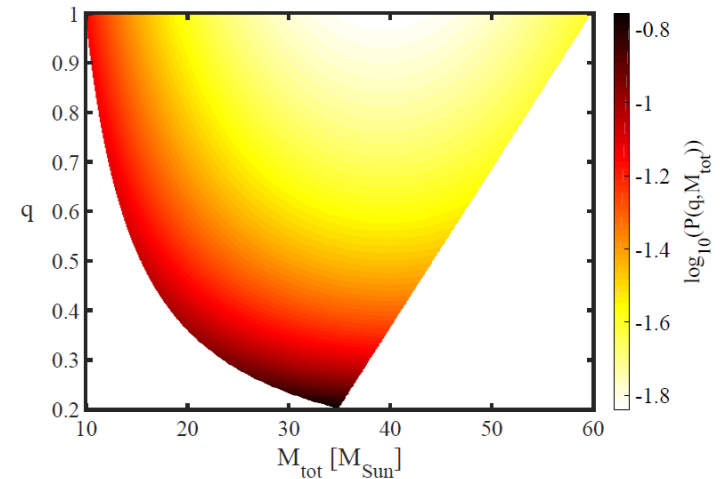
$$-(m_1 + m_2)^2 \frac{\partial^2}{\partial m_1 \partial m_2} \ln \mathcal{R}(m_1, m_2, t)$$

= **4** in globular clusters (*needs revision)

= **1.4 ... -5** for GW capture binaries in galactic nuclei

= **1.4** for GW capture binaries in collisionless systems

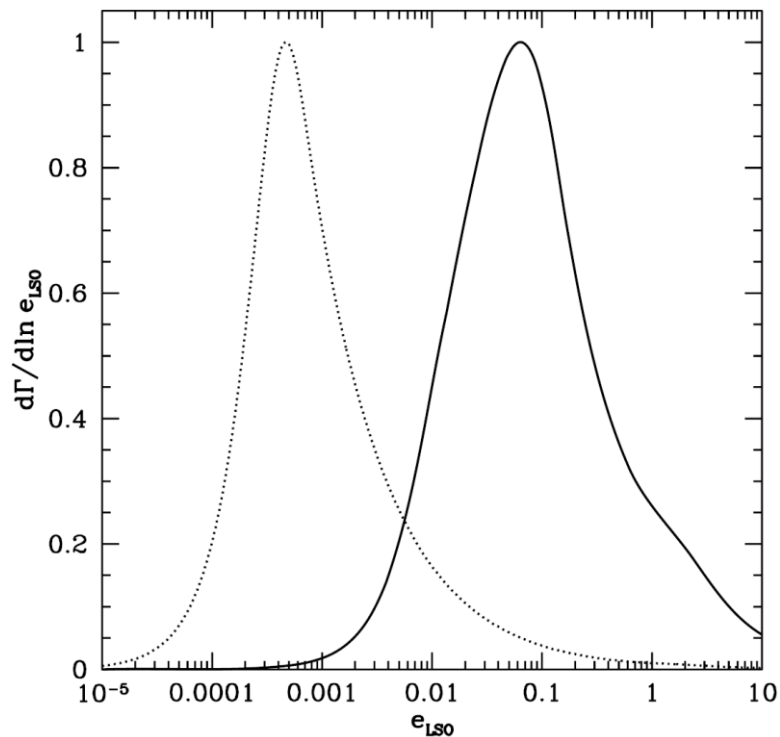
= **1** for PBH binaries formed in early universe



Eccentricity distribution for GW capture binaries

Velocity dispersion \rightarrow maximum initial pericenter distance $r_p/M \rightarrow$ eccentricity at merger

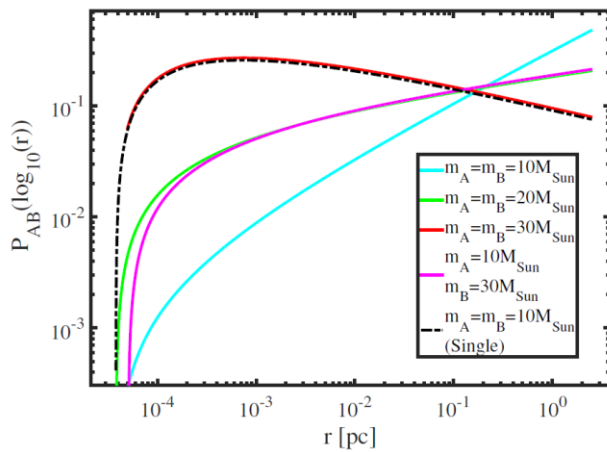
$$\sigma \sim 258 \frac{\text{km}}{\text{s}} (4\eta)^{1/2} \left(\frac{e_{\text{LSO,peak}}}{0.01} \right)^{35/32}$$



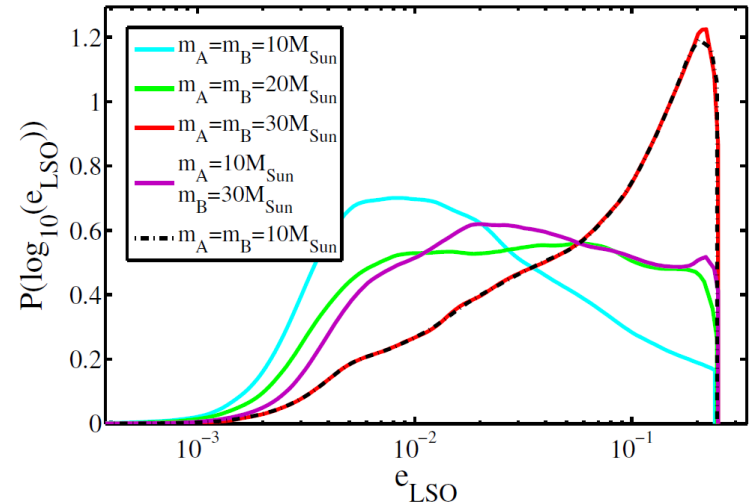
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$$\sigma \sim 258 \frac{\text{km}}{\text{s}} (4\eta)^{1/2} \left(\frac{e_{\text{LSO,peak}}}{0.01} \right)^{35/32}$$



radial distribution of mergers
shows mass segregation

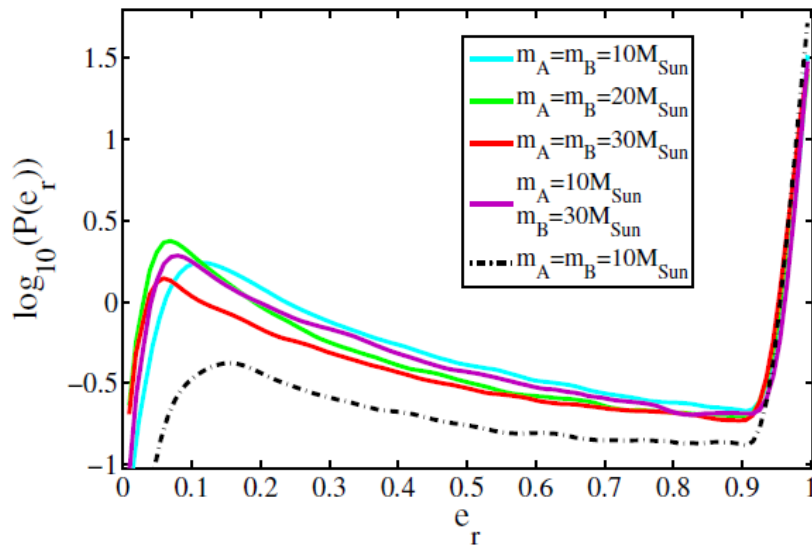


\rightarrow Eccentricity distribution
reveals mass segregation

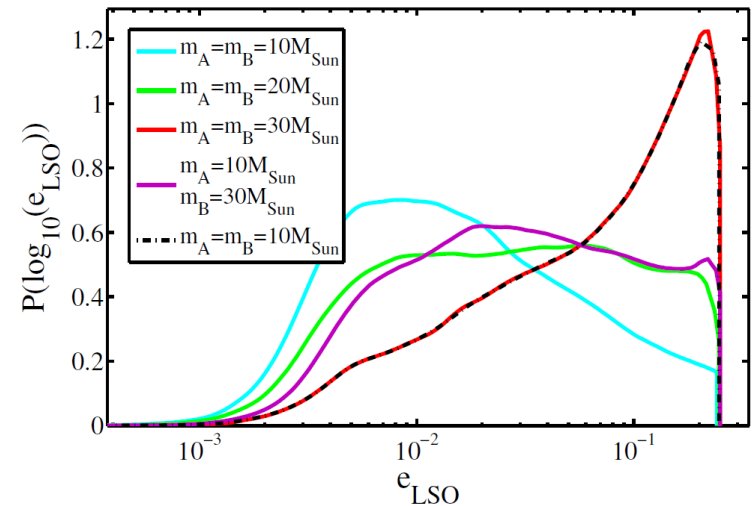
Eccentricity distribution for GW capture binaries

Velocity dispersion \rightarrow maximum initial pericenter distance $r_p/M \rightarrow$ eccentricity at merger

$$\sigma \sim 258 \frac{\text{km}}{\text{s}} (4\eta)^{1/2} \left(\frac{e_{\text{LSO,peak}}}{0.01} \right)^{35/32}$$



Eccentricity distribution when ALIGO first sees it (design sensitivity)

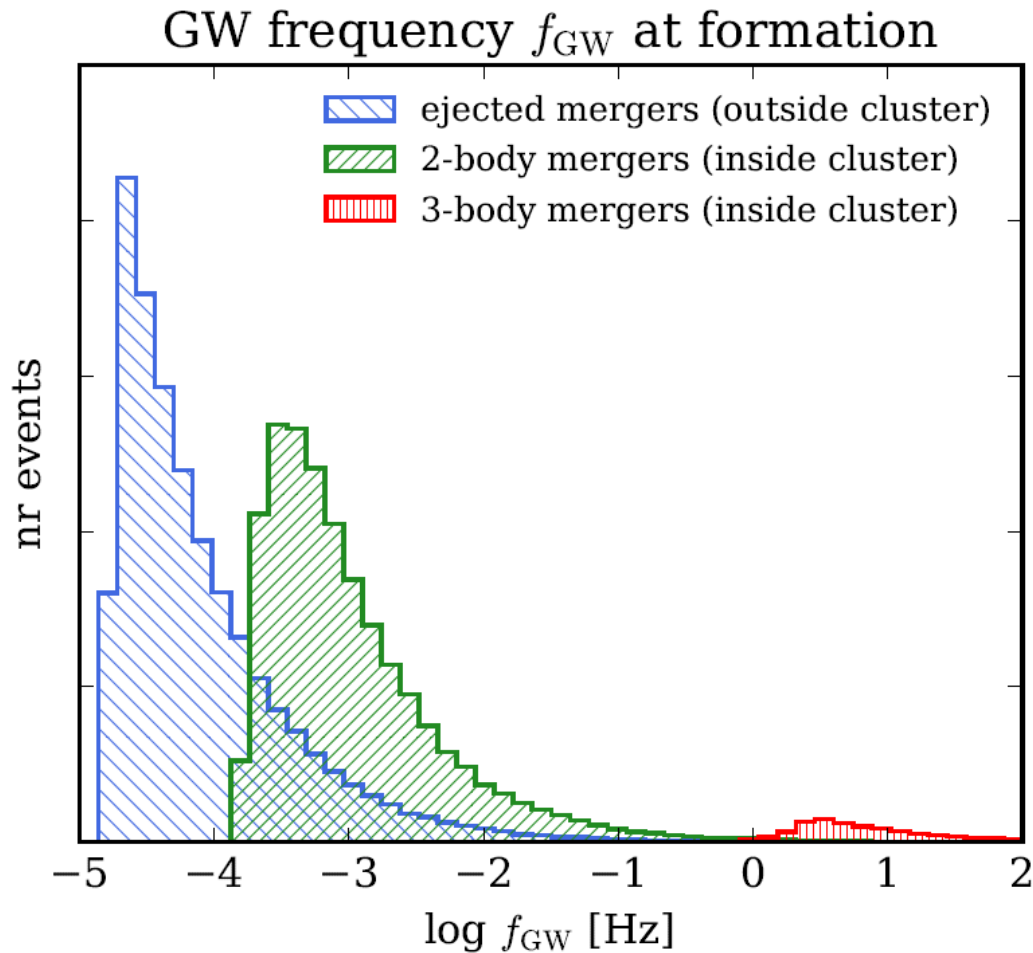


\rightarrow **Eccentricity distribution** reveals **mass segregation**

cf. measurement accuracy $\Delta e_{\text{LSO}} \sim 10^{-2}-10^{-3}$

$30M_{\text{Sun}}+30M_{\text{Sun}}$ @ 1Gpc

Eccentricity distribution for merging globular cluster binaries

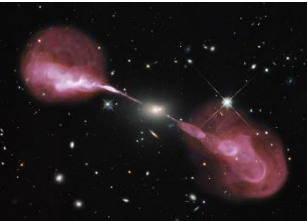


Eccentric sources: rates from different channels

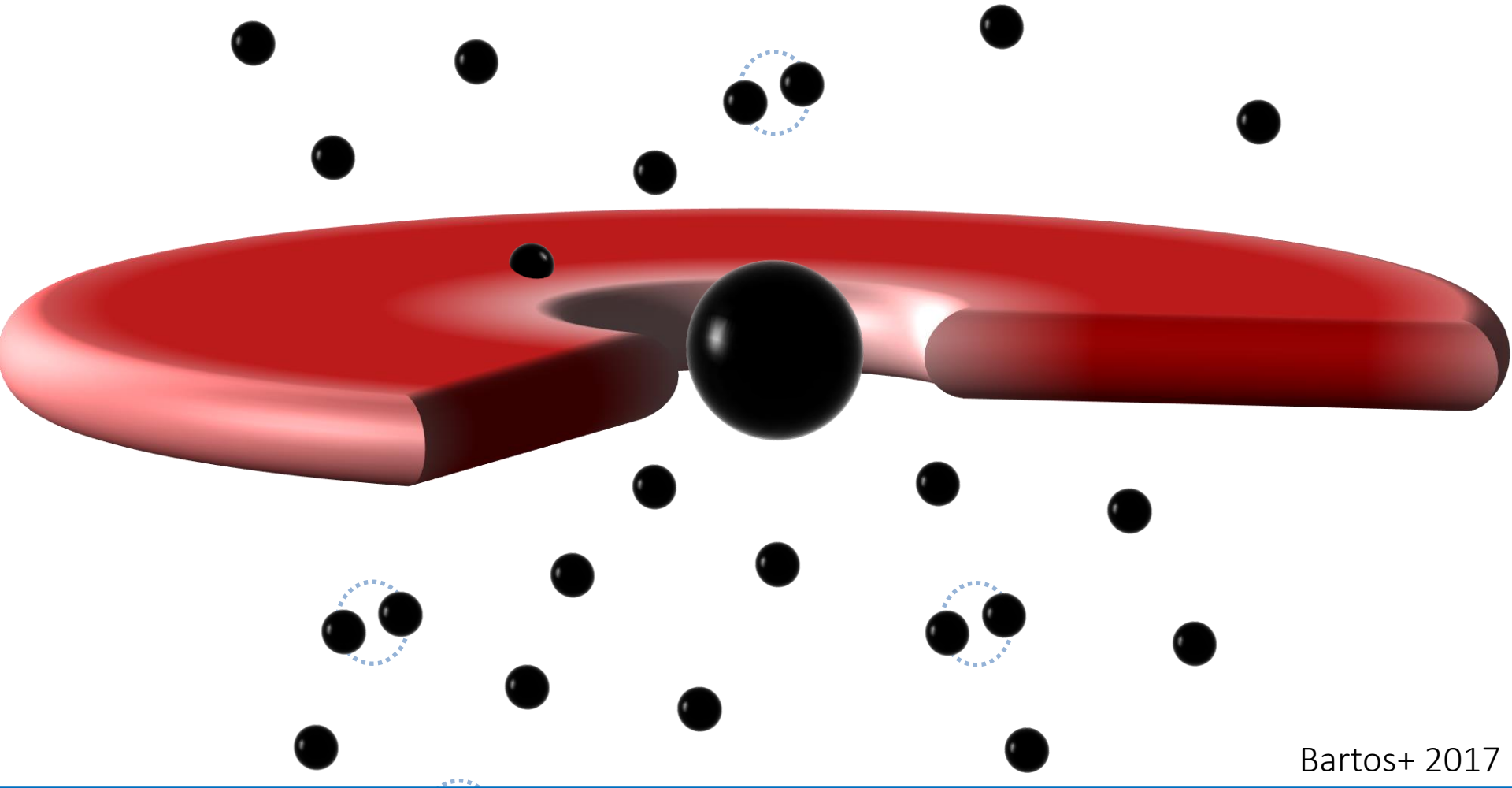
	GW capture (single-single interactions)	Hierarchical triples (Kozai-Lidov effect)	Binary-single interactions
Nuclear star clusters	0.01-0.1 (this work) 0.8 (O'Leary+09) 0.02 (Tsang 2013)	? (Hoang+2018)	0? (Antonini & Rasio 2016)
Globular clusters	?	0.04 (Antonini+2016)	0.05 - 0.5 (Samsing+2018, Rodriguez+2018)
Galactic field	0?	0.002 - 0.1 ? (Silsbee&Tremaine 2017) 0.01 - 0.04 (Antonini+2017)	?



Mergers with EM counterparts

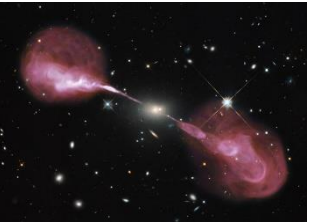


GW sources in active galactic nuclei

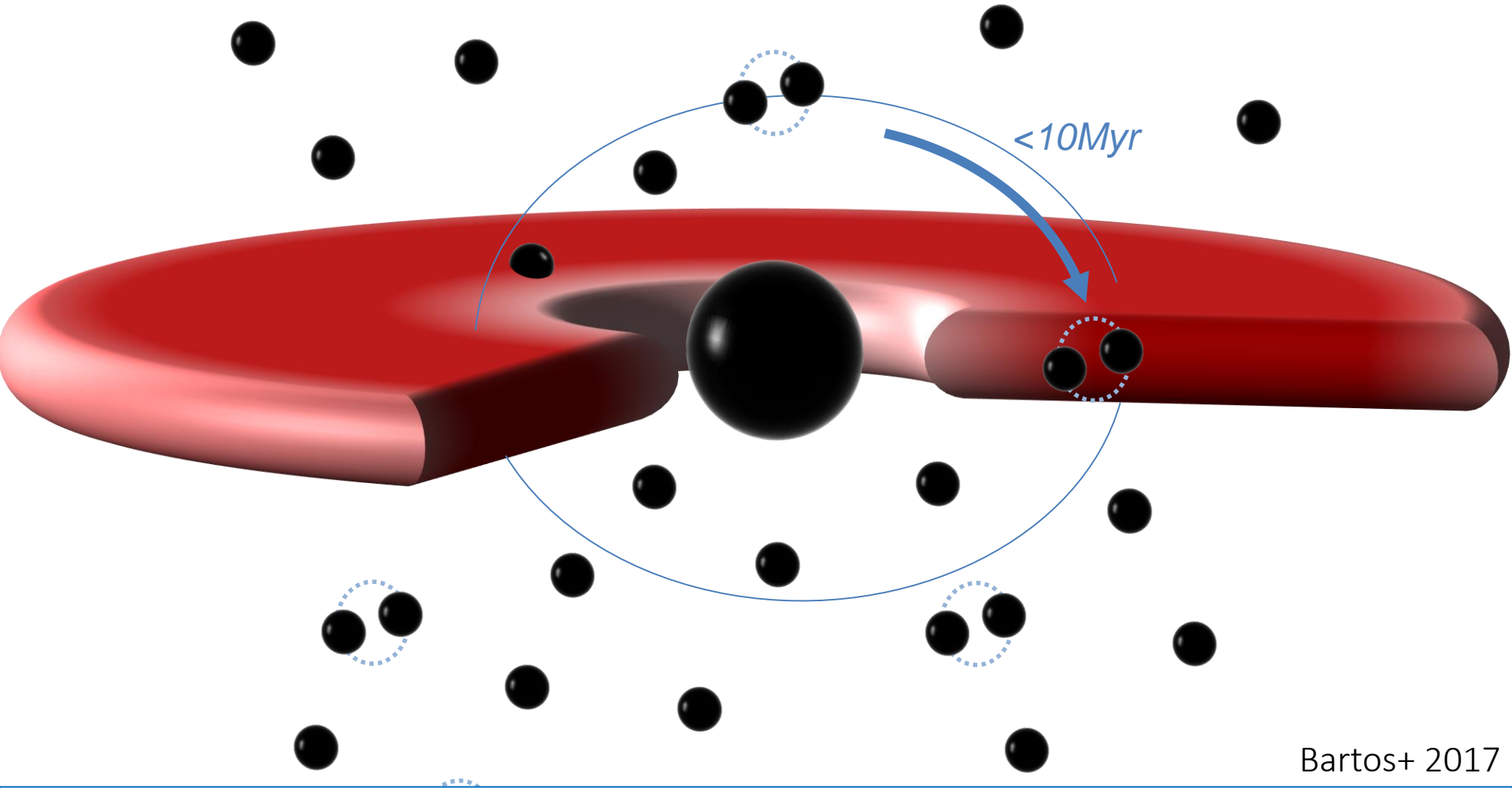


Bartos+ 2017

There are large amounts of gas at the centers of 1% of galaxies (AGN).⁵¹

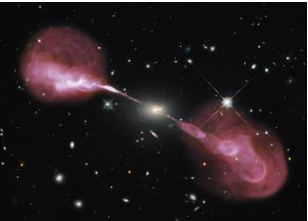


GW sources in active galactic nuclei

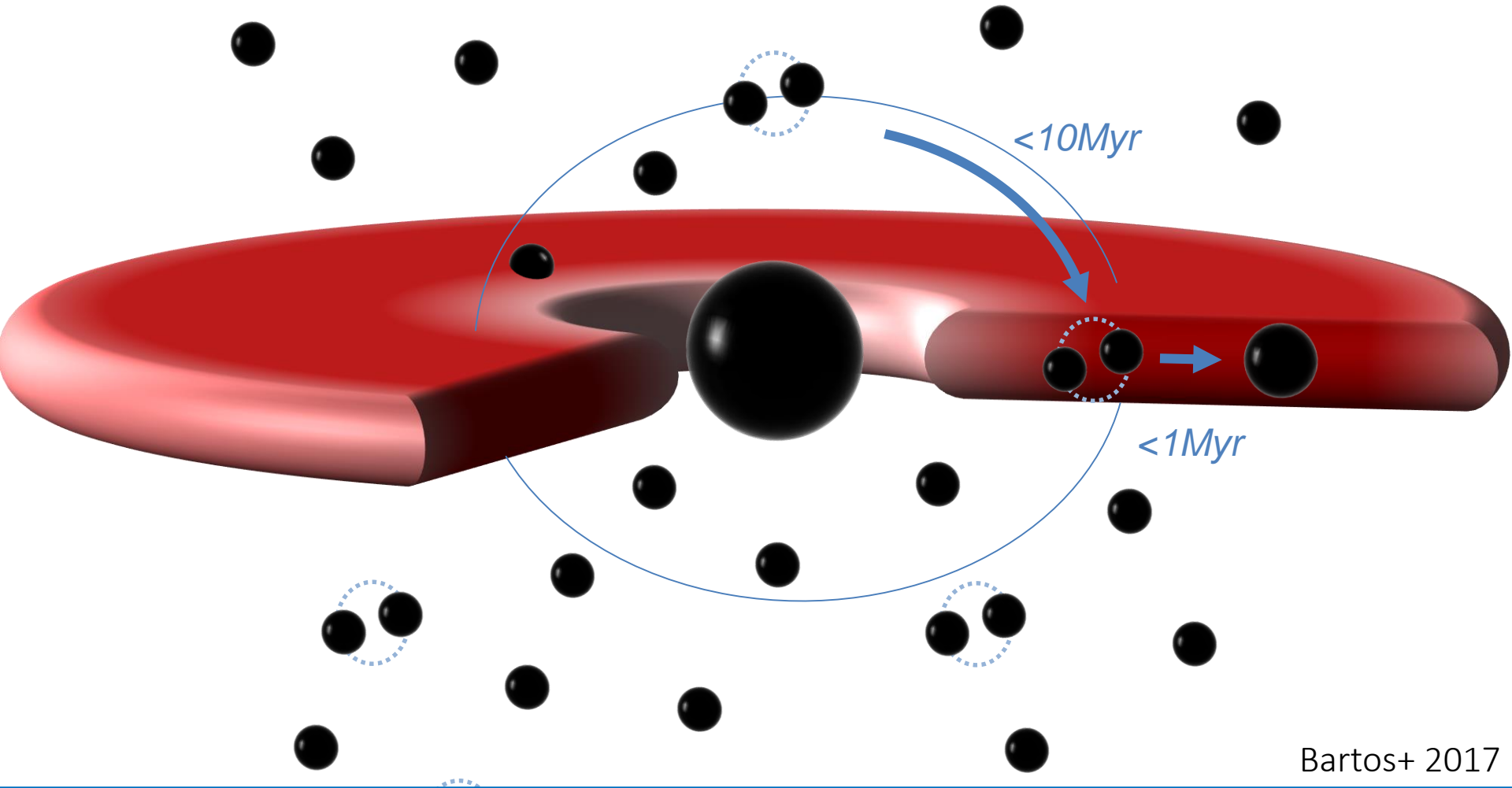


Bartos+ 2017

Get captured by the disk...

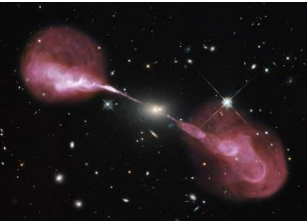


GW sources in active galactic nuclei

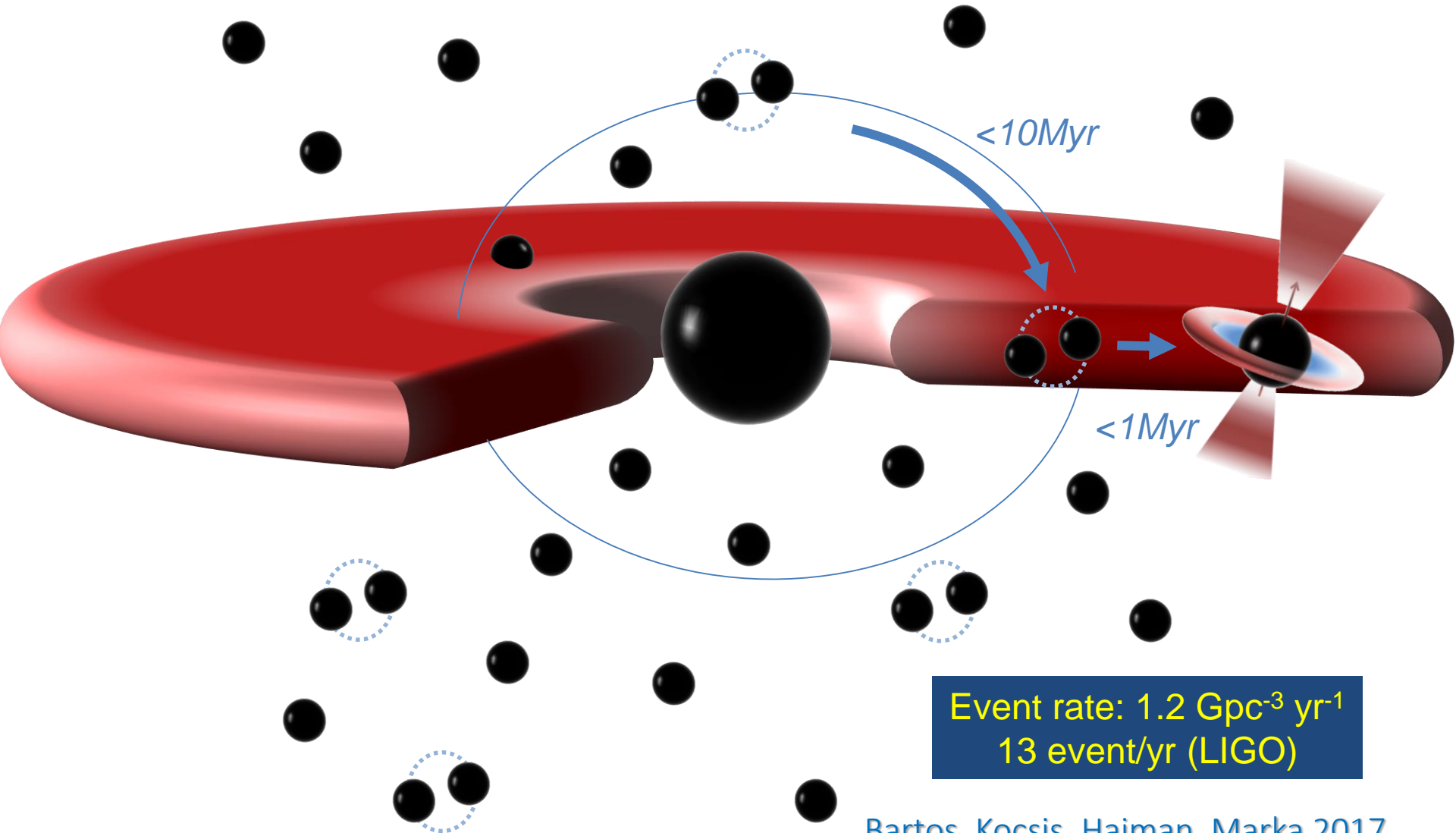


Bartos+ 2017

...and then quickly merge due to dynamical friction on the gas



GW sources in active galactic nuclei

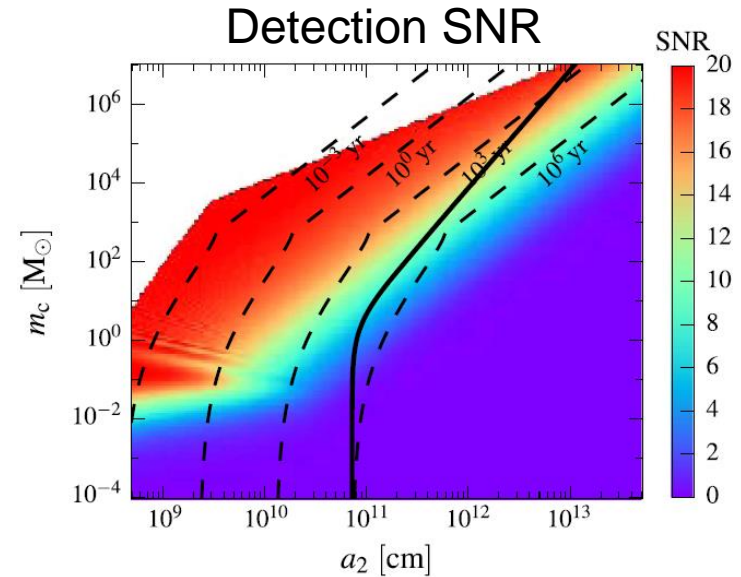
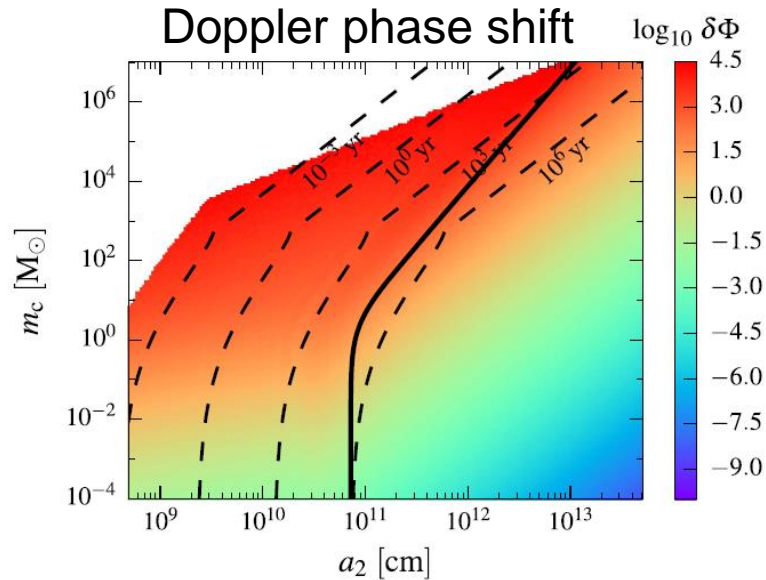
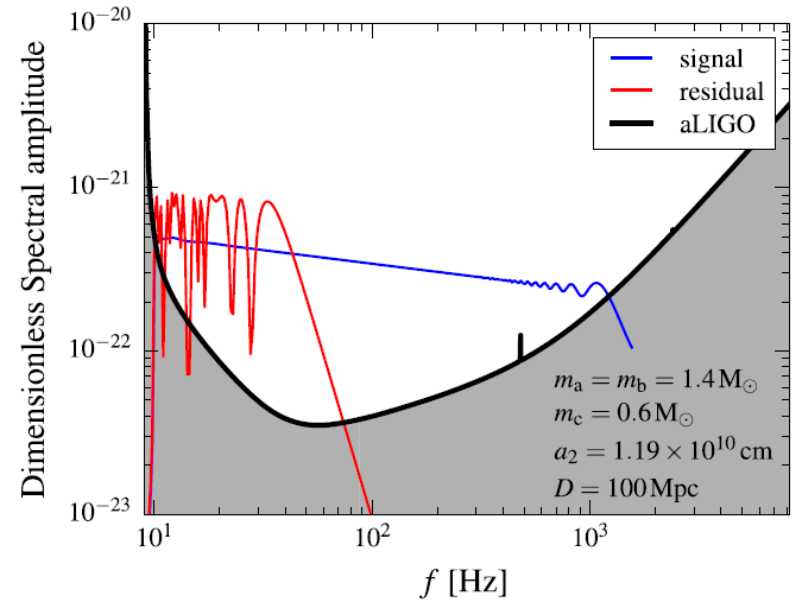
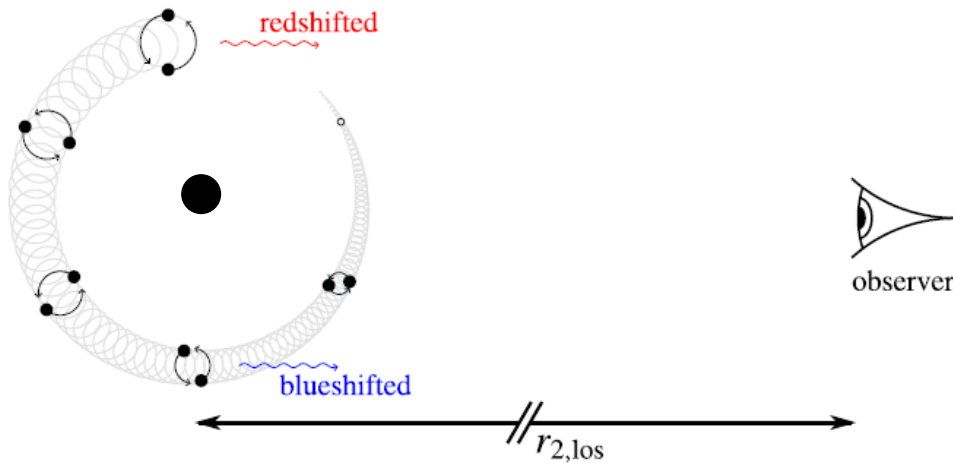


Event rate: $1.2 \text{ Gpc}^{-3} \text{ yr}^{-1}$
13 event/yr (LIGO)

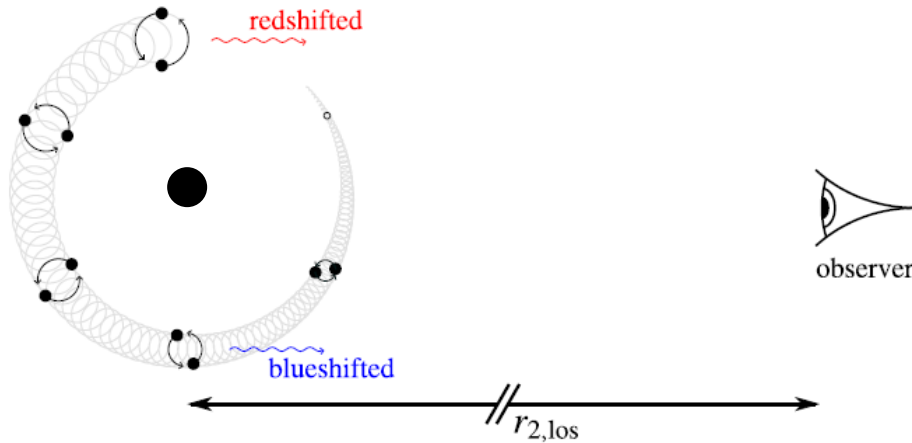
Bartos, Kocsis, Haiman, Marka 2017
Stone, Metzger, Haiman 2017

**Smoking gun signatures
to identify origin of source**

SMBH/AGN source with LIGO



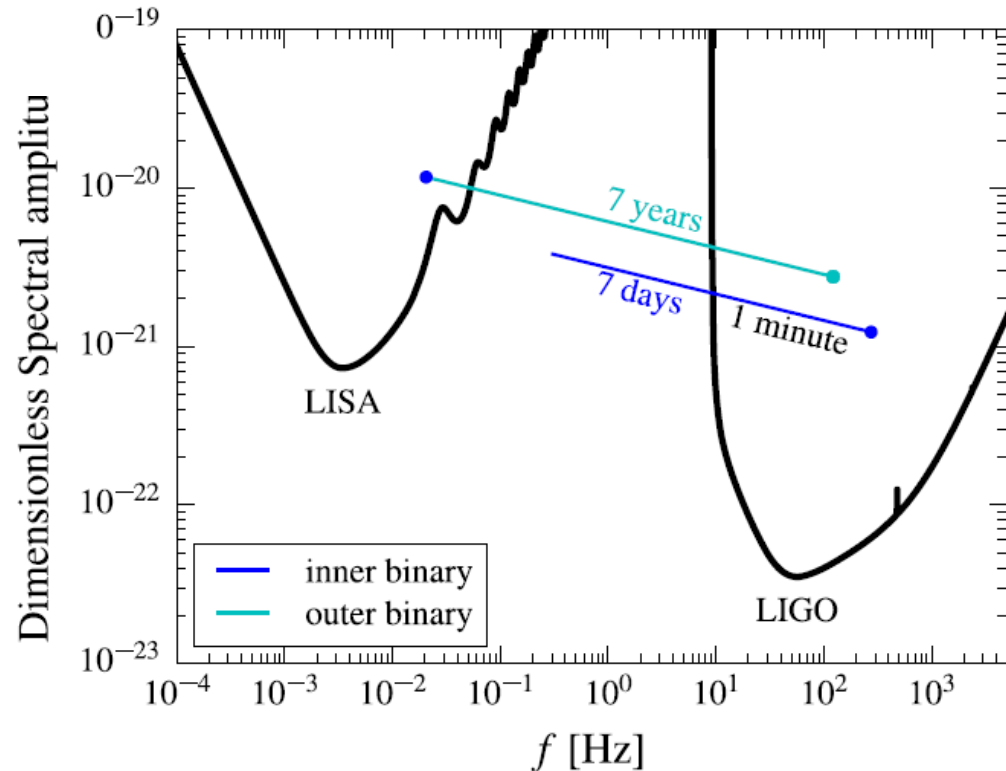
SMBH/AGN source with LIGO+LISA



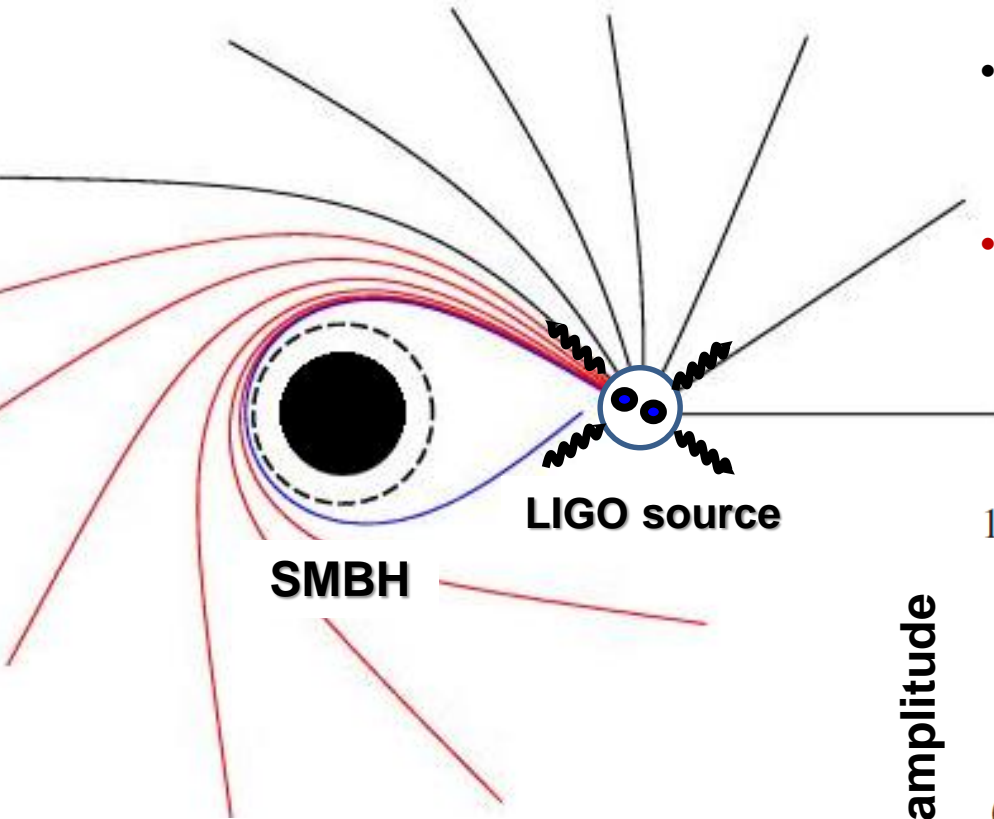
- LISA+LIGO coincident detection of triple inspiral
- LIGO detection of GW mass loss
- LISA detection of GW mass loss
- Later: LIGO detection of merger (if stellar-mass triple)

Test of general relativity

see also Sesana (2016), Inayoshi+ (2017)



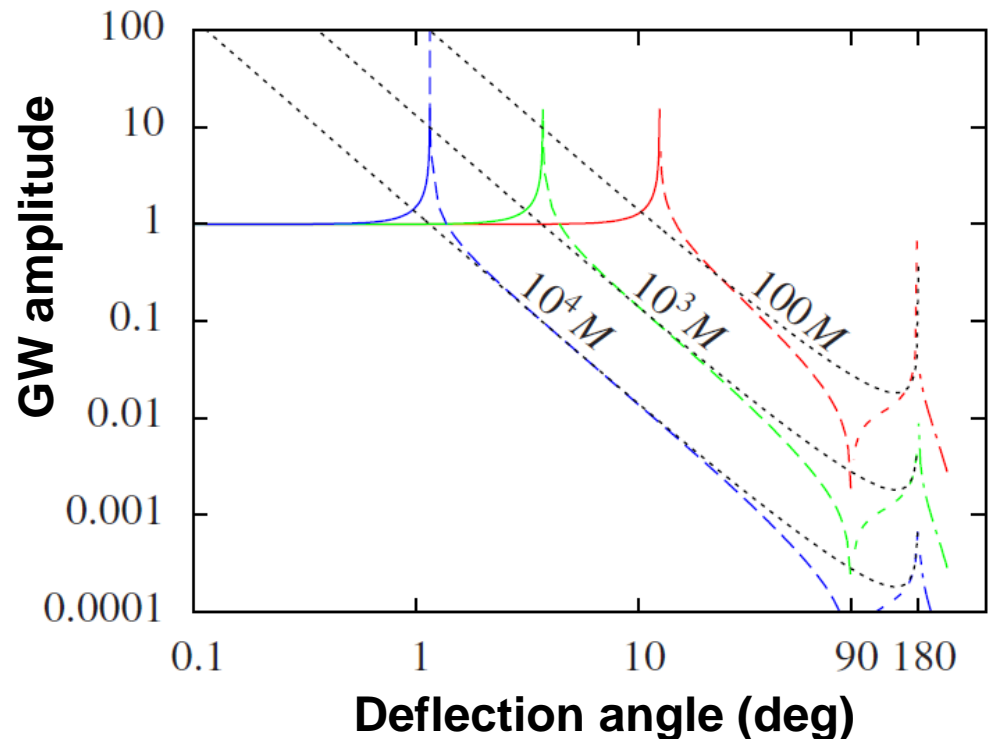
GW echos



- GW rays are deflected around supermassive black holes
- Echo amplitude depends on distance to SMBH and deflection angle

GW echo arrives in

$$14\text{h} \times (1 - \cos \alpha) M_6 (r / 10^4 M)$$



**What about
intermediate mass black holes?**

$100 M_{\text{Sun}} - 10^5 M_{\text{Sun}}$

intermediate mass black holes

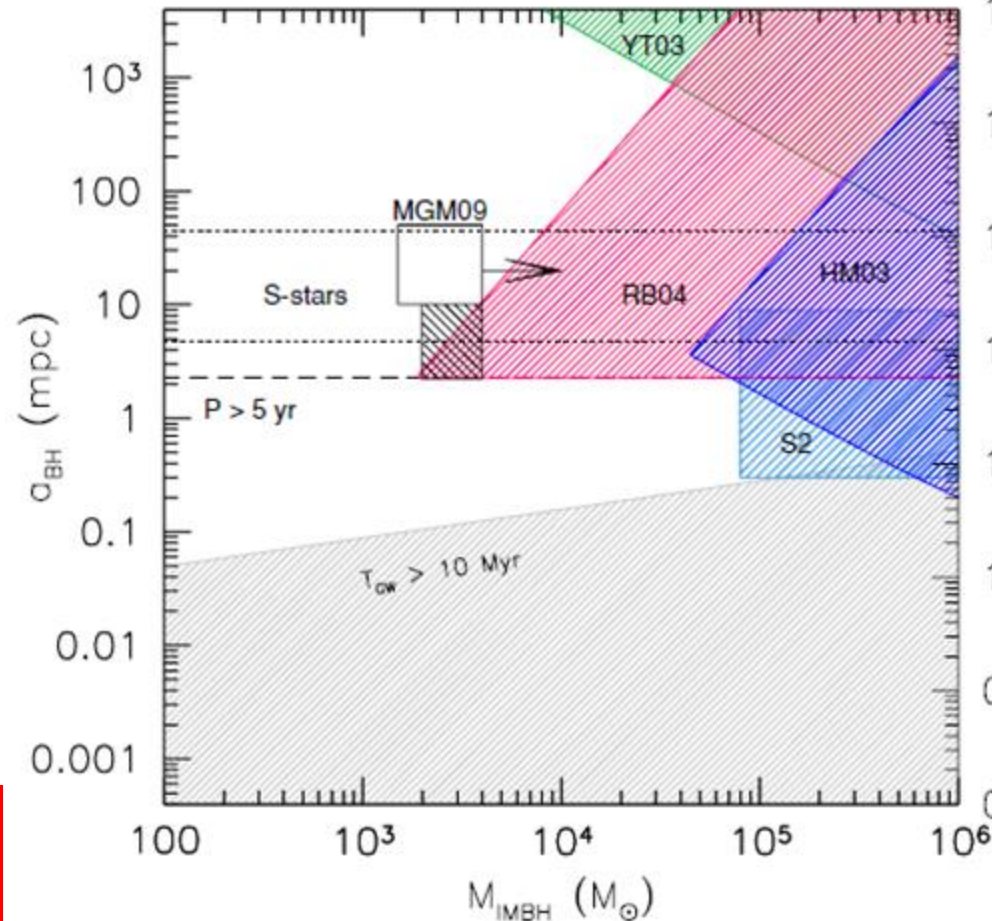
Theory

Formation

- Early universe:
 - collapse of the first stars (Madau & Reese '01)
- Globular clusters
 - runaway collisions (Portegies Zwart & McMillan '02)
 - mergers of stellar mass black holes (Miller & Hamilton '02)
 - dynamical friction
 - IMBH deposited in the galactic center
- In accretion disks (Goodman & Tan 04', McKernan+ '12, '14; Leigh+)

~ 50 IMBHs within 10 pc
~ 8,000 IMBHs within 1kpc

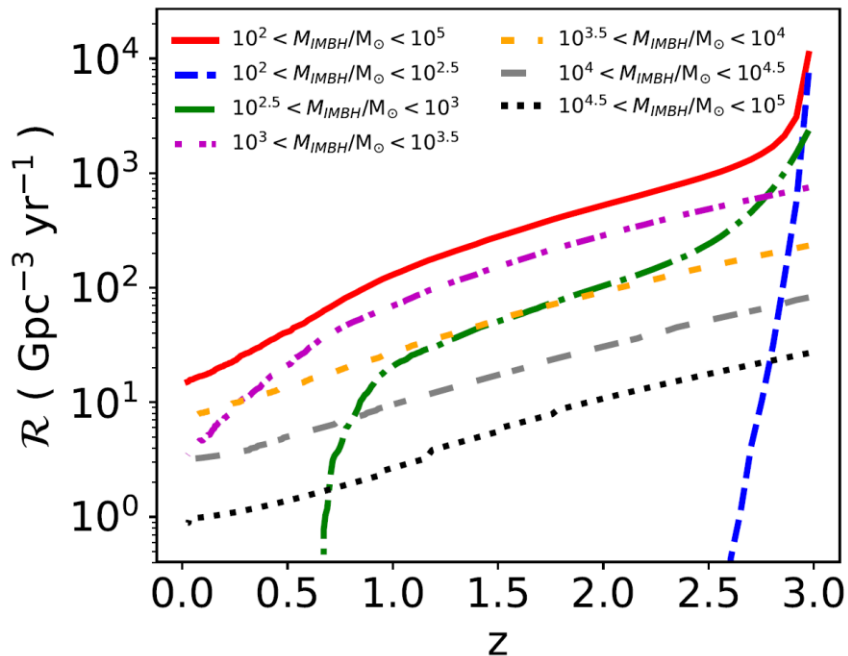
Observational constraints



Yu & Tremaine (2003)
Gualandris & Merritt (2009)

GWs from intermediate mass black holes

IMBH + BH mergers in globular clusters



$M < 300 M_{\text{sun}} @ z > 2.6$ ☹️

$>300 M_{\text{sun}}$ mergers are closer ($z > 0.6$)
but currently not detectable due to
low-frequency noise

Advanced LIGO @ design sensitivity
and LISA should see them 😊 😊

Take-away

- **New ideas are needed** to identify the most common source
 - fallback driven mergers ?
 - disrupted globular clusters ?
 - black hole disks?
- Discriminate LIGO sources using **2D mass distribution**
 - 4 for globular clusters
 - 2 for galactic nuclei
 - 1 for primordial black holes
- **Eccentricity** measurable at design sensitivity
 - Delta e ~ 0.01
- **Smoking gun signatures** in some cases
 - Doppler phase
 - GW echo for a few percent of these
- **IMBH discovery expected** at LIGO design sensitivity

$$-(m_1 + m_2)^2 \frac{\partial^2}{\partial m_1 \partial m_2} \ln \mathcal{R}(m_1, m_2, t).$$

